

**Math Vector Library  
Reference Manual (C/C++)  
DD-00002-010**

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# 1 About this Guide

## 1.1 Legal Information

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## 1.3 Introduction

This manual describes the *Application Programming Interface* (API) of the *Math Vector Library* for the C and C++ programming language families.

## 1.4 Audience for This Guide

The audience of this guide is assumed to be C or C++ programmers who understand the basic concepts of at least one of the aforementioned programming languages.

Familiarity with pointer based arrays in C/C++ is strongly recommended.

## 1.5 How to Use This Guide

This guide first describes some general programming details of the library and then documents each function individually.

The documentation for each function applies both the *single* and *double* precision versions. The former can be differentiated by a suffix letter *f*.

## 1.6 Conventions Used in This Guide

*x*  
Normal math typesetting represents a normal variable.

**x**  
Bold math typesetting represents a vector.

Mono  
Monospace typesetting represents C function names, variables or data types.

## 2 Overview

### 2.1 Introduction

The *Math Vector Library* is a high-performance function library with vectorized versions of standard mathematical functions. The functions can operate both on dense and strided vectors, the latter can be supplied individually for result and operand vectors. Stride only executes the function on every  $n$ -th element leaving the elements in between untouched.

This manual describes the *Application Programming Interface (API)* of the mathematics vector functions.

### 2.2 Thread Safety

All routines in the library are completely thread-safe, as long as the data supplied in arguments is exclusive to the current thread.

### 2.3 SIMD/SPMD Unit Usage

This library makes excessive use of *Single Instruction Multiple Data (SIMD)* or *Single program Multiple Data (SPMD)* style extensions of the respective processor platform. It thereby abides by the standard system calling conventions when utilizing such.

### 2.4 Performance Characteristics

All subroutines in this library have a performance characteristic of  $O(n)$ . The routines may have different execution profiles depending upon the arguments supplied.



## 3 Utility

### 3.1 mvecver - Version query

```
#include <mvec.h>
```

```
void mvecver(int *major, int *minor);
```

Queries the version of the library and stores the *major* and *minor* version numbers in the respective arguments.

#### 3.1.1 Parameters

**MAJOR - INTEGER EXIT:** The major version number of the library.

**MINOR - INTEGER EXIT:** The minor version number of the library

## 4 Rounding

### 4.1 vfloor - Vector round down

```
#include <mvec.h>
```

```
void vfloor (int n, double *y, int incy, const double *x, int incx);  
void vfloorf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$  this function rounds the elements of  $\mathbf{x}$  to the nearest integral part less or equal than  $|\mathbf{x}|$  and stores the result in  $\mathbf{y}$ .

#### 4.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

## 4.2 `vceil` - Vector round up

```
#include <mvec.h>
```

```
void vceil (int n, double *y, int incy, const double *x, int incx);  
void vceilf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** and a result vector **y** this function rounds the elements of **x** to the nearest integral part greater or equal than  $|x|$  and stores the result in **y**.

### 4.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector **y**.

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.

*CONSTRAINT:*  $\text{incx} > 0$ .

### 4.3 `vtrunc` - Vector truncate

```
#include <mvec.h>
```

```
void vtrunc (int n, double *y, int incy, const double *x, int incx);  
void vtruncf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$  this function truncates the elements of  $\mathbf{x}$  to the nearest integral part lower or equal than  $|\mathbf{x}|$  and stores the result in  $\mathbf{y}$ .

#### 4.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 4.4 vround - Vector rounding

```
#include <mvec.h>
```

```
void vround (int n, double *y, int incy, const double *x, int incx);  
void vroundf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** and a result vector **y** this function rounds the elements of **x** to the nearest integral part and stores the result in **y**.

### 4.4.1 Parameters

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector **y**.  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 5 Roots

### 5.1 vsqrt - Vector square root $\sqrt{\mathbf{x}}$

```
#include <mvec.h>
```

```
void vsqrt (int n, double *y, int incy, const double *x, int incx);
void vsqrtf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sqrt{\mathbf{x}}$$

#### 5.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

## 5.2 *vrsqrt* - Vector reciprocal square root $1/\sqrt{\mathbf{x}}$

```
#include <mvec.h>
```

```
void vrsqrt (int n, double *y, int incy, const double *x, int incx);  
void vrsqrtf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \frac{1}{\sqrt{\mathbf{x}}}$$

### 5.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

### 5.3 `vcbirt` - Vector cube root $\sqrt[3]{\mathbf{x}}$

```
#include <mvec.h>
```

```
void vcbirt (int n, double *y, int incy, const double *x, int incx);  
void vcbirtf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sqrt[3]{\mathbf{x}}$$

#### 5.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .



## 5.4 vrcbrt - Vector reciprocal cube root $1/\sqrt[3]{\mathbf{x}}$

```
#include <mvec.h>
```

```
void vrcbrt (int n, double *y, int incy, const double *x, int incx);  
void vrcbrtf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \frac{1}{\sqrt[3]{\mathbf{x}}}$$

### 5.4.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 6 Trigonometric Functions

### 6.1 vsin - Vector sine $\sin(\mathbf{x})$

```
#include <mvec.h>
```

```
void vsin (int n, double *y, int incy, const double *x, int incx);
void vsinf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin(\mathbf{x})$$

#### 6.1.1 Parameters

**N - INTEGER** *ENTRY*: Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT*:  $n \geq 1$ .

**Y - ARRAY OF REAL** *EXIT*: Result vector  $\mathbf{y}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT*:  $\text{incy} > 0$ .

**X - ARRAY OF REAL** *ENTRY*: Input vector  $\mathbf{x}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT*:  $\text{incx} > 0$ .

## 6.2 `vcos` - Vector cosine $\cos(\mathbf{x})$

```
#include <mvec.h>
```

```
void vcos (int n, double *y, int incy, const double *x, int incx);  
void vcosf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos(\mathbf{x})$$

### 6.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

### 6.3 vtan - Vector tangent tan(**x**)

```
#include <mvec.h>
```

```
void vtan (int n, double *y, int incy, const double *x, int incx);  
void vtanf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** and a result vector **y**, this function computes:

$$\mathbf{y} = \tan(\mathbf{x})$$

#### 6.3.1 Parameters

**N** - **INTEGER ENTRY**: Number of elements of **x** and **y**.

*CONSTRAINT*:  $n \geq 1$ .

**Y** - **ARRAY OF REAL EXIT**: Result vector **y**.

*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT*: Must not overlap with array **x**.

**INCY** - **INTEGER ENTRY**: Stride for the vector **y**.

*CONSTRAINT*:  $\text{incy} > 0$ .

**X** - **ARRAY OF REAL ENTRY**: Input vector **x**.

*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT*: Must not overlap with array **y**.

**INCX** - **INTEGER ENTRY**: Stride for the vector **x**.

*CONSTRAINT*:  $\text{incx} > 0$ .

## 6.4 vasin - Vector arcsine $\sin^{-1}(\mathbf{x})$

```
#include <mvec.h>
```

```
void vasin (int n, double *y, int incy, const double *x, int incx);  
void vasinf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin^{-1}(\mathbf{x})$$

### 6.4.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.5 vacos - Vector arccosine  $\cos^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vacos (int n, double *y, int incy, const double *x, int incx);
void vacosf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos^{-1}(\mathbf{x})$$

**6.5.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.6 vatan - Vector arctangent  $\tan^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vatan (int n, double *y, int incy, const double *x, int incx);  
void vatanf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tan^{-1}(\mathbf{x})$$

**6.6.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.7 vatan2 - Vector arctangent  $\tan^{-1}(\mathbf{x}/\mathbf{y})$** 

```
#include <mvec.h>
```

```
void vatan2 (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);
void vatan2f(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes:

$$\mathbf{z} = \tan^{-1}(\mathbf{x}/\mathbf{y})$$

**6.7.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .  
*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .



## 6.8 vsind - Vector sine sin(**x**) (degrees)

```
#include <mvec.h>
```

```
void vsind (int n, double *y, int incy, const double *x, int incx);  
void vsindf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** with angles in degrees (°) and a result vector **y**, this function computes:

$$\mathbf{y} = \sin(\mathbf{x})$$

### 6.8.1 Parameters

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector **y**.  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 6.9 `vcosd` - Vector cosine $\cos(\mathbf{x})$ (degrees)

```
#include <mvec.h>
```

```
void vcosd (int n, double *y, int incy, const double *x, int incx);  
void vcosdf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  with angles in degrees ( $^\circ$ ) and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos(\mathbf{x})$$

### 6.9.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.10 vtand - Vector tangent tan(**x**) (degrees)**

```
#include <mvec.h>
```

```
void vtand (int n, double *y, int incy, const double *x, int incx);  
void vtandf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** with angles in degrees (°) and a result vector **y**, this function computes:

$$\mathbf{y} = \tan(\mathbf{x})$$

**6.10.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector **y**.

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.

*CONSTRAINT:*  $\text{incx} > 0$ .

**6.11 *vasind* - Vector arcsine  $\sin^{-1}(\mathbf{x})$  (degrees)**

```
#include <mvec.h>
```

```
void vasind (int n, double *y, int incy, const double *x, int incx);  
void vasindf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin^{-1}(\mathbf{x})$$

**6.11.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.12 vacosd - Vector arccosine  $\cos^{-1}(\mathbf{x})$  (degrees)**

```
#include <mvec.h>
```

```
void vacosd (int n, double *y, int incy, const double *x, int incx);  
void vacosdf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos^{-1}(\mathbf{x})$$

**6.12.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.13 `vatand` - Vector arctangent  $\tan^{-1}(\mathbf{x})$  (degrees)**

```
#include <mvec.h>
```

```
void vatand (int n, double *y, int incy, const double *x, int incx);
void vatandf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tan^{-1}(\mathbf{x})$$

**6.13.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.14 vsinpi - Vector sine  $\sin(\pi\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vsinpi (int n, double *y, int incy, const double *x, int incx);  
void vsinpif(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  with angles in degrees ( $^\circ$ ) and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin(\pi\mathbf{x})$$

**6.14.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**6.15 *vcospi* - Vector cosine  $\cos(\pi\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcospi (int n, double *y, int incy, const double *x, int incx);  
void vcospif(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  with angles in degrees ( $^\circ$ ) and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos(\pi\mathbf{x})$$

**6.15.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .



**6.16 vtanpi - Vector tangent  $\tan(\pi\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vtanpi (int n, double *y, int incy, const double *x, int incx);  
void vtanpif(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  with angles in degrees ( $^\circ$ ) and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tan(\pi\mathbf{x})$$

**6.16.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**6.17** *vasinpi* - Vector arcsine  $\sin^{-1}(\mathbf{x})/\pi$ 

```
#include <mvec.h>
```

```
void vasinpi (int n, double *y, int incy, const double *x, int incx);  
void vasinpif(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin^{-1}(\mathbf{x})/\pi$$

**6.17.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.18 vacospi - Vector arccosine  $\cos^{-1}(\mathbf{x})/\pi$** 

```
#include <mvec.h>
```

```
void vacospi (int n, double *y, int incy, const double *x, int incx);  
void vacospif(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos^{-1}(\mathbf{x})/\pi$$

**6.18.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**6.19 vatanpi - Vector arctangent  $\tan^{-1}(\mathbf{x})/\pi$** 

```
#include <mvec.h>
```

```
void vatanpi (int n, double *y, int incy, const double *x, int incx);
void vatanpif(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tan^{-1}(\mathbf{x})/\pi$$

**6.19.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 7 Hypergeometric Functions

### 7.1 vsinh - Vector hypergeometric sine $\sinh(\mathbf{x})$

```
#include <mvec.h>
```

```
void vsinh (int n, double *y, int incy, const double *x, int incx);
void vsinhf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sinh(\mathbf{x})$$

#### 7.1.1 Parameters

**N - INTEGER** *ENTRY*: Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT*:  $n \geq 1$ .

**Y - ARRAY OF REAL** *EXIT*: Result vector  $\mathbf{y}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT*:  $\text{incy} > 0$ .

**X - ARRAY OF REAL** *ENTRY*: Input vector  $\mathbf{x}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT*:  $\text{incx} > 0$ .

## 7.2 `vcosh` - Vector hypergeometric cosine cosh( $\mathbf{x}$ )

```
#include <mvec.h>
```

```
void vcosh (int n, double *y, int incy, const double *x, int incx);  
void vcoshf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cosh(\mathbf{x})$$

### 7.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

### 7.3 vtanh - Vector hypergeometric tangent tanh(**x**)

```
#include <mvec.h>
```

```
void vtanh (int n, double *y, int incy, const double *x, int incx);  
void vtanhf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** and a result vector **y**, this function computes:

$$\mathbf{y} = \tanh(\mathbf{x})$$

#### 7.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector **y**.  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.  
*CONSTRAINT:*  $\text{incx} > 0$ .

**7.4 *vasinh* - Vector hypergeometric arcsine  $\sinh^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vasinh (int n, double *y, int incy, const double *x, int incx);  
void vasinhf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sinh^{-1}(\mathbf{x})$$

**7.4.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .



**7.5 vacosh - Vector hypergeometric arccosine cosh<sup>-1</sup>(**x**)**

```
#include <mvec.h>
```

```
void vacosh (int n, double *y, int incy, const double *x, int incx);
void vacoshf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector **x** and a result vector **y**, this function computes:

$$\mathbf{y} = \cosh^{-1}(\mathbf{x})$$

**7.5.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector **y**.  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.  
*CONSTRAINT:*  $\text{incx} > 0$ .

**7.6 vatanh - Vector hypergeometric arctangent  $\tanh^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vatanh (int n, double *y, int incy, const double *x, int incx);  
void vatanhf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tanh^{-1}(\mathbf{x})$$

**7.6.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 8 Exponentials and Logarithms

### 8.1 vexp - Vector exponential $e^{\mathbf{x}}$

```
#include <mvec.h>
```

```
void vexp (int n, double *y, int incy, const double *x, int incx);
void vexpf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = e^{\mathbf{x}}$$

#### 8.1.1 Parameters

**N - INTEGER** *ENTRY*: Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT*:  $n \geq 1$ .

**Y - ARRAY OF REAL** *EXIT*: Result vector  $\mathbf{y}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT*:  $\text{incy} > 0$ .

**X - ARRAY OF REAL** *ENTRY*: Input vector  $\mathbf{x}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT*:  $\text{incx} > 0$ .

## 8.2 `vexpm1` - Vector exponential $e^{\mathbf{x}} - 1$

```
#include <mvec.h>
```

```
void vexpm1 (int n, double *y, int incy, const double *x, int incx);  
void vexpm1f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = e^{\mathbf{x}} - 1$$

### 8.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

### 8.3 vexp2 - Vector binary exponential $2^x$

```
#include <mvec.h>
```

```
void vexp2 (int n, double *y, int incy, const double *x, int incx);  
void vexp2f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = 2^{\mathbf{x}}$$

#### 8.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 8.4 vlog - Vector logarithm $\log(\mathbf{x})$

```
#include <mvec.h>
```

```
void vlog (int n, double *y, int incy, const double *x, int incx);  
void vlogf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \log(\mathbf{x})$$

### 8.4.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 8.5 vlog2 - Vector binary logarithm $\log_2(\mathbf{x})$

```
#include <mvec.h>
```

```
void vlog2 (int n, double *y, int incy, const double *x, int incx);  
void vlog2f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \log_2(\mathbf{x})$$

### 8.5.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**8.6 vlog10 - Vector base-10 logarithm  $\log_{10}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vlog10 (int n, double *y, int incy, const double *x, int incx);  
void vlog10f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \log_{10}(\mathbf{x})$$

**8.6.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .



## 8.7 vlog1p - Vector logarithm $\log(\mathbf{x} + 1)$

```
#include <mvec.h>
```

```
void vlog1p (int n, double *y, int incy, const double *x, int incx);  
void vlog1pf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \log(\mathbf{x} + 1)$$

### 8.7.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**8.8 vpow - Vector power  $\mathbf{x}^y$** 

```
#include <mvec.h>
```

```
void vpow (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);
void vpowf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given an input vectors  $\mathbf{x}$  and  $\mathbf{y}$  as well as a result vector  $\mathbf{z}$ , this function computes:

$$\mathbf{z} = \mathbf{x}^y$$

**8.8.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .  
*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**8.9 vpows - Vector power scalar exponent $x^y$** 

```
#include <mvec.h>
```

```
void vpows (int n, double *z, int incz, const double *x, int incx, double y);
void vpowsf(int n, float *z, int incz, const float *x, int incx, float y);
```

Given an input vectors  $\mathbf{x}$  and a scalar value  $y$  as well as a result vector  $\mathbf{z}$ , this function computes:

$$\mathbf{z} = \mathbf{x}^y$$

**8.9.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .  
*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - REAL ENTRY:** Exponentiation value  $y$ .

**8.10 vmod - Vector modulus mod(**x**,**y**)**

```
#include <mvec.h>
```

```
void vmod (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);
void vmodf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given an input vectors **x** and **y** as well as a result vector **z**, this function computes:

$$\mathbf{z} = \text{mod}(\mathbf{x}, \mathbf{y})$$

**8.10.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of **x**, **y** and **z**.  
*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector **z**.  
*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.  
*CONSTRAINT:* Must not overlap with array **x** or **y**.

**INCZ - INTEGER ENTRY:** Stride for the vector **z**.  
*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector **x**.  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array **z** or **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.  
*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector **y**.  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array **z** or **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.  
*CONSTRAINT:*  $\text{incy} > 0$ .

## 9 Special Functions

### 9.1 `verf` - Vector error function `erf(x)`

```
#include <mvec.h>
```

```
void verf (int n, double *y, int incy, const double *x, int incx);
void verff(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \text{erf}(\mathbf{x})$$

#### 9.1.1 Parameters

**N - INTEGER** *ENTRY*: Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT*:  $n \geq 1$ .

**Y - ARRAY OF REAL** *EXIT*: Result vector  $\mathbf{y}$ .

*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT*: Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT*:  $\text{incy} > 0$ .

**X - ARRAY OF REAL** *ENTRY*: Input vector  $\mathbf{x}$ .

*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT*: Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT*:  $\text{incx} > 0$ .

## 9.2 *verfc* - Vector complementary error function $\text{erfc}(\mathbf{x})$

```
#include <mvec.h>
```

```
void verfc (int n, double *y, int incy, const double *x, int incx);  
void verfcf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \text{erfc}(\mathbf{x})$$

### 9.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

### 9.3 vbesj0 - Vector Bessel Function $J_0(\mathbf{x})$

```
#include <mvec.h>
```

```
void vbesj0 (int n, double *y, int incy, const double *x, int incx);  
void vbesj0f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = J_0(\mathbf{x})$$

#### 9.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 9.4 `vbesy0` - Vector Bessel Function $Y_0(\mathbf{x})$

```
#include <mvec.h>
```

```
void vbesy0 (int n, double *y, int incy, const double *x, int incx);  
void vbesy0f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = Y_0(\mathbf{x})$$

### 9.4.1 Parameters

**N** - **INTEGER** *ENTRY*: Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT*:  $n \geq 1$ .

**Y** - **ARRAY OF REAL** *EXIT*: Result vector  $\mathbf{y}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{x}$ .

**INCY** - **INTEGER** *ENTRY*: Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT*:  $\text{incy} > 0$ .

**X** - **ARRAY OF REAL** *ENTRY*: Input vector  $\mathbf{x}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{y}$ .

**INCX** - **INTEGER** *ENTRY*: Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT*:  $\text{incx} > 0$ .



## 9.5 vbesj1 - Vector Bessel Function $J_1(\mathbf{x})$

```
#include <mvec.h>
```

```
void vbesj1 (int n, double *y, int incy, const double *x, int incx);  
void vbesj1f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = J_1(\mathbf{x})$$

### 9.5.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**9.6 *vbesy1* - Vector Bessel Function  $Y_1(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vbesy1 (int n, double *y, int incy, const double *x, int incx);  
void vbesy1f(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = Y_1(\mathbf{x})$$

**9.6.1 Parameters**

**N - INTEGER** *ENTRY*: Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT*:  $n \geq 1$ .

**Y - ARRAY OF REAL** *EXIT*: Result vector  $\mathbf{y}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT*:  $\text{incy} > 0$ .

**X - ARRAY OF REAL** *ENTRY*: Input vector  $\mathbf{x}$ .  
*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT*: Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER** *ENTRY*: Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT*:  $\text{incx} > 0$ .

**9.7 vbesjn - Vector Bessel Function  $J_n(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vbesjn (int n, double *y, int incy, int k, const double *x, int incx);
void vbesjnf(int n, float *y, int incy, int k, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$ , an order  $k$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = J_k(\mathbf{x})$$

**9.7.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**K - INTEGER ENTRY:** Order  $k$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**9.8 vbesyn - Vector Bessel Function  $Y_n(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vbesyn (int n, double *y, int incy, int k, const double *x, int incx);
void vbesynf(int n, float *y, int incy, int k, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$ , an order  $k$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = Y_k(\mathbf{x})$$

**9.8.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**K - INTEGER ENTRY:** Order  $k$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

## 9.9 vlgamma - Vector Log-Gamma $\log\Gamma(\mathbf{x})$

```
#include <mvec.h>
```

```
void vlgamma (int n, double *y, int incy, const double *x, int incx);  
void vlgammaf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \log\Gamma(\mathbf{x})$$

### 9.9.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

## 10 Other Functions

### 10.1 vabs - Vector absolute value $|\mathbf{x}|$

```
#include <mvec.h>
```

```
void vabs (int n, double *y, int incy, const double *x, int incx);
void vabsf(int n, float *y, int incy, const float *x, int incx);
```

Given an input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = |\mathbf{x}|$$

#### 10.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**10.2** *vhypot* - Vector euclidean distance  $\sqrt{\mathbf{x}^2 + \mathbf{y}^2}$ 

```
#include <mvec.h>
```

```
void vhypot (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);
void vhypotf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes:

$$\mathbf{z} = \sqrt{\mathbf{x}^2 + \mathbf{y}^2}$$

**10.2.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

### 10.3 vrem - Vector remainder

```
#include <mvec.h>
```

```
void vrem (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);  
void vremf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes the remainder of dividing  $x$  by  $y$  and stores the result in  $z$ .

#### 10.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .



## 11 Arithmetic Functions

### 11.1 vadd - Vector addition $\mathbf{x} + \mathbf{y}$

```
#include <mvec.h>
```

```
void vadd (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);
void vaddf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x} + \mathbf{y}$$

#### 11.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

## 11.2 vsadd - Vector scalar addition $\mathbf{x} + \alpha$

```
#include <mvec.h>
```

```
void vsadd (int n, double *y, int incy, const double *x, int incx, double a);  
void vsaddf (int n, float *y, int incy, const float *x, int incx, float a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \mathbf{x} + \alpha$$

### 11.2.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - REAL ENTRY:** Scalar constant  $\alpha$ .

### 11.3 vsub - Vector subtraction $\mathbf{x} - \mathbf{y}$

```
#include <mvec.h>
```

```
void vsub (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);  
void vsubf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x} - \mathbf{y}$$

#### 11.3.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**11.4 vssub - Vector scalar subtraction  $\mathbf{x} - \alpha$** 

```
#include <mvec.h>
```

```
void vssub (int n, double *y, int incy, const double *x, int incx, double a);  
void vssubf(int n, float *y, int incy, const float *x, int incx, float a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \mathbf{x} - \alpha$$

**11.4.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - REAL ENTRY:** Scalar constant  $\alpha$ .

## 11.5 vmul - Vector multiplication $\mathbf{xy}$

```
#include <mvec.h>
```

```
void vmul (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);  
void vmulf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{xy}$$

### 11.5.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

## 11.6 vsmul - Vector scalar multiplication $\alpha \mathbf{x}$

```
#include <mvec.h>
```

```
void vsmul (int n, double *y, int incy, const double *x, int incx, double a);  
void vsmulf(int n, float *y, int incy, const float *x, int incx, float a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \alpha \mathbf{x}$$

### 11.6.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**A - REAL ENTRY:** Scalar constant  $\alpha$ .

**11.7 *vdiv* - Vector division  $\mathbf{x}/\mathbf{y}$** 

```
#include <mvec.h>
```

```
void vdiv (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);
void vdivf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x}/\mathbf{y}$$

**11.7.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF REAL EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**11.8 vsdiv - Vector scalar division  $\mathbf{x}/\alpha$** 

```
#include <mvec.h>
```

```
void vsdiv (int n, double *y, int incy, const double *x, int incx, double a);  
void vsdivf(int n, float *y, int incy, const float *x, int incx, float a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \mathbf{x}/\alpha$$

**11.8.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF REAL ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - REAL ENTRY:** Scalar constant  $\alpha$ .

*CONSTRAINT:*  $\alpha \neq 0$ .



## 11.9 *vrecp* - Vector reciprocal 1/**x**

```
#include <mvec.h>
```

```
void vrecp (int n, double *z, int incz, const double *x, int incx, const double *y, int incy);  
void vrecpf(int n, float *z, int incz, const float *x, int incx, const float *y, int incy);
```

Given input vector **x** and a result vector **y**, this function computes

$$\mathbf{y} = 1/\mathbf{x}$$

### 11.9.1 Parameters

**N** - **INTEGER ENTRY**: Number of elements of **x** and **y**.  
*CONSTRAINT*:  $n \geq 1$ .

**Y** - **ARRAY OF REAL EXIT**: Result vector **y**.  
*CONSTRAINT*: Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT*: Must not overlap with array **x**.

**INCY** - **INTEGER ENTRY**: Stride for the vector **y**.  
*CONSTRAINT*:  $\text{incy} > 0$ .

**X** - **ARRAY OF REAL ENTRY**: Input vector **x**.  
*CONSTRAINT*: Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT*: Must not overlap with array **y**.

**INCX** - **INTEGER ENTRY**: Stride for the vector **x**.  
*CONSTRAINT*:  $\text{incx} > 0$ .

## 12 Complex Numbers

### 12.1 vcreal - Vector complex real component $\text{Re}(\mathbf{x})$

```
#include <mvec.h>
```

```
void vcreal (int n, double *y, int incy, const double complex *x, int incx);
void vcrealf(int n, float *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a real result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \text{Re}(\mathbf{x})$$

Where  $\mathbf{x} \in \mathbb{C}$  and  $\mathbf{y} \in \mathbb{R}$ .

#### 12.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**12.2 *vcimag* - Vector complex imaginary component  $\text{Im}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcimag (int n, double *y, int incy, const double complex *x, int incx);
void vcimagf(int n, float *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a real result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \text{Im}(\mathbf{x})$$

Where  $\mathbf{x} \in \mathbb{C}$  and  $\mathbf{y} \in \mathbb{R}$ .

**12.2.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.3 vcabs - Vector complex absolute value  $|\mathbf{x}|$** 

```
#include <mvec.h>
```

```
void vcabs (int n, double *y, int incy, const double complex *x, int incx);
void vcabsf(int n, float *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = |\mathbf{x}|$$

Where  $\mathbf{x} \in \mathbb{C}$  and  $\mathbf{y} \in \mathbb{R}$ .

**12.3.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.4 *vcarg* - Vector complex argument  $\arg(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcarg (int n, double *y, int incy, const double complex *x, int incx);
void vcargf(int n, float *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \arg(\mathbf{x})$$

Where  $\mathbf{x} \in \mathbb{C}$  and  $\mathbf{y} \in \mathbb{R}$ .

**12.4.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF REAL EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.5 vconj - Vector complex conjugate  $\bar{\mathbf{x}}$** 

```
#include <mvec.h>
```

```
void vconj (int n, double complex *y, int incy, const double complex *x, int incx);
void vconjf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \bar{\mathbf{x}}$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**12.5.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.6 *vcproj* - Vector complex Riemann sphere projection *proj(x)***

```
#include <mvec.h>
```

```
void vcproj (int n, double complex *y, int incy, const double complex *x, int incx);
void vcprojf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \text{proj}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**12.6.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.7 *vcexp* - Vector complex exponentiation  $\exp(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcexp (int n, double complex *y, int incy, const double complex *x, int incx);
void vcexpf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \exp(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**12.7.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .



**12.8 `vclog` - Vector complex logarithm  $\log(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vclog (int n, double complex *y, int incy, const double complex *x, int incx);
void vclogf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \log(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**12.8.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.9 vcsqrt - Vector complex square root  $\sqrt{\mathbf{x}}$** 

```
#include <mvec.h>
```

```
void vcsqrt (int n, double complex *y, int incy, const double complex *x, int incx);
void vcsqrtf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sqrt{\mathbf{x}}$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**12.9.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**12.10 vcpow - Vector complex power  $\mathbf{x}^y$** 

```
#include <mvec.h>
```

```
void vcpow (int n, double complex *z, int incz, const double complex *x, int incx, const double complex *y, int incy)
void vcpowf (int n, float complex *z, int incz, const float complex *x, int incx, const float complex *y, int incy)
```

Given an input vectors  $\mathbf{x}$  and  $\mathbf{y}$  as well as a result vector  $\mathbf{z}$ , this function computes:

$$\mathbf{z} = \mathbf{x}^{\mathbf{y}}$$

Where  $\mathbf{x}, \mathbf{y}, \mathbf{z} \in \mathbb{C}$ .

**12.10.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**12.11 vcpows - Vector complex power scalar exponent  $\mathbf{x}^y$** 

```
#include <mvec.h>
```

```
void vcpows (int n, double complex *z, int incz, const double complex *x, int incx, double complex y);
void vcpowsf(int n, float complex *z, int incz, const float complex *x, int incx, float complex y);
```

Given an input vectors  $\mathbf{x}$  and a scalar value  $y$  as well as a result vector  $\mathbf{z}$ , this function computes:

$$\mathbf{z} = \mathbf{x}^y$$

**12.11.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - COMPLEX ENTRY:** Exponentiation value  $y$ .

## 13 Complex Trigonometric Functions

### 13.1 vcsin - Vector complex sine $\sin(\mathbf{x})$

```
#include <mvec.h>
```

```
void vcsin (int n, double complex *y, int incy, const double complex *x, int incx);
void vcsinf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

#### 13.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .  
*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .  
*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .  
*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.  
*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .  
*CONSTRAINT:*  $\text{incx} > 0$ .

**13.2 `vccos` - Vector complex cosine  $\cos(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vccos (int n, double complex *y, int incy, const double complex *x, int incx);
void vccosf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.2.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.3 vctan - Vector complex tangent tan(x)**

```
#include <mvec.h>
```

```
void vctan (int n, double complex *y, int incy, const double complex *x, int incx);
void vctanf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tan(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.3.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.4 *vcasin* - Vector complex arcsine  $\sin^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcasin (int n, double complex *y, int incy, const double complex *x, int incx);
void vcasinf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sin^{-1}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.4.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .



**13.5 *vcacos* - Vector complex arccosine  $\cos^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcacos (int n, double complex *y, int incy, const double complex *x, int incx);
void vccosf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cos^{-1}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.5.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.6 vcatan - Vector complex arctangent  $\tan^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcatan (int n, double complex *y, int incy, const double complex *x, int incx);
void vcatanf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tan^{-1}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.6.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.7 *vcsinh* - Vector complex hyperbolic sine  $\sinh(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcsinh (int n, double complex *y, int incy, const double complex *x, int incx);
void vcsinhf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sinh(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.7.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.8 vccosh - Vector complex hyperbolic cosine cosh(**x**)**

```
#include <mvec.h>
```

```
void vccosh (int n, double complex *y, int incy, const double complex *x, int incx);
void vccoshf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector **x** and a result vector **y**, this function computes:

$$\mathbf{y} = \cosh(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.8.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of **x** and **y**.

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector **y**.

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array **x**.

**INCY - INTEGER ENTRY:** Stride for the vector **y**.

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector **x**.

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array **y**.

**INCX - INTEGER ENTRY:** Stride for the vector **x**.

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.9 `vctanh` - Vector complex hyperbolic tangent  $\tanh(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vctanh (int n, double complex *y, int incy, const double complex *x, int incx);
void vctanhf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tanh(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.9.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.10 `vcasinh` - Vector complex hyperbolic arcsine  $\sinh^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcasinh (int n, double complex *y, int incy, const double complex *x, int incx);  
void vcasinhf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \sinh^{-1}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.10.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.11 *vcacosh* - Vector complex hyperbolic arccosine  $\cosh^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcacosh (int n, double complex *y, int incy, const double complex *x, int incx);
void vcacoshf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \cosh^{-1}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.11.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**13.12 vcatanh - Vector complex hyperbolic arctangent  $\tanh^{-1}(\mathbf{x})$** 

```
#include <mvec.h>
```

```
void vcatanh (int n, double complex *y, int incy, const double complex *x, int incx);
void vcatanhf(int n, float complex *y, int incy, const float complex *x, int incx);
```

Given a complex input vector  $\mathbf{x}$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \tanh^{-1}(\mathbf{x})$$

Where  $\mathbf{x}, \mathbf{y} \in \mathbb{C}$ .

**13.12.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .



## 14 Complex Arithmetic

### 14.1 v<sub>c</sub>add - Vector complex addition $\mathbf{x} + \mathbf{y}$

```
#include <mvec.h>
```

```
void vcadd (int n, double complex *z, int incz, const double complex *x, int incx, const double complex *y, int incy)
void vcaddf (int n, float complex *z, int incz, const float complex *x, int incx, const float complex *y, int incy)
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x} + \mathbf{y}$$

#### 14.1.1 Parameters

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**14.2 *vcsadd* - Vector complex scalar subtraction  $\mathbf{x} + \alpha$** 

```
#include <mvec.h>
```

```
void vcsadd (int n, double complex *y, int incy, const double complex *x, int incx, double complex a);
void vcsaddf(int n, float complex *y, int incy, const float complex *x, int incx, float complex a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \mathbf{x} + \alpha$$

**14.2.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - COMPLEX ENTRY:** Scalar constant  $\alpha$ .

**14.3 *vcs*ub - Vector complex subtraction  $\mathbf{x} - \mathbf{y}$** 

```
#include <mvec.h>
```

```
void vcsub (int n, double complex *z, int incz, const double complex *x, int incx, const double complex *y, int incy)
void vcsuf (int n, float complex *z, int incz, const float complex *x, int incx, const float complex *y, int incy)
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x} - \mathbf{y}$$

**14.3.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**14.4 vcsub - Vector complex scalar subtraction  $\mathbf{x} - \alpha$** 

```
#include <mvec.h>
```

```
void vcsub (int n, double complex *y, int incy, const double complex *x, int incx, double complex a);  
void vcsubf(int n, float complex *y, int incy, const float complex *x, int incx, float complex a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \mathbf{x} - \alpha$$

**14.4.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - COMPLEX ENTRY:** Scalar constant  $\alpha$ .

**14.5 vcmul - Vector complex multiplication  $\mathbf{xy}$** 

```
#include <mvec.h>
```

```
void vcmul (int n, double complex *z, int incz, const double complex *x, int incx, const double complex *y, int incy)
void vcmulf(int n, float complex *z, int incz, const float complex *x, int incx, const float complex *y, int incy)
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{xy}$$

**14.5.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**14.6 `vcsmul` - Vector complex scalar multiplication  $\alpha \mathbf{x}$** 

```
#include <mvec.h>
```

```
void vcsmul (int n, double complex *y, int incy, const double complex *x, int incx, double complex a);  
void vcsmlf(int n, float complex *y, int incy, const float complex *x, int incx, float complex a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \alpha \mathbf{x}$$

**14.6.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - COMPLEX ENTRY:** Scalar constant  $\alpha$ .

**14.7 vcmulc - Vector complex conjugate multiplication  $\mathbf{x}\bar{\mathbf{y}}$** 

```
#include <mvec.h>
```

```
void vcmulc (int n, double complex *z, int incz, const double complex *x, int incx, const double complex *y, int incy)
void vcmulcf(int n, float complex *z, int incz, const float complex *x, int incx, const float complex *y, int incy)
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x}\bar{\mathbf{y}}$$

**14.7.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**14.8 `vcdiv` - Vector complex division  $\mathbf{x}/\mathbf{y}$** 

```
#include <mvec.h>
```

```
void vcdiv (int n, double complex *z, int incz, const double complex *x, int incx, const double complex *y, int incy)
void vcdivf(int n, float complex *z, int incz, const float complex *x, int incx, const float complex *y, int incy)
```

Given input vectors  $\mathbf{x}$  and  $\mathbf{y}$  and a result vector  $\mathbf{z}$ , this function computes

$$\mathbf{z} = \mathbf{x}/\mathbf{y}$$

**14.8.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{z}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Z - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{z}$ .

*CONSTRAINT:* Must contain  $n \times \text{incz}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$  or  $\mathbf{y}$ .

**INCZ - INTEGER ENTRY:** Stride for the vector  $\mathbf{z}$ .

*CONSTRAINT:*  $\text{incz} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**Y - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{z}$  or  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .



**14.9 *vcdiv* - Vector complex scalar division  $\mathbf{x}/\alpha$** 

```
#include <mvec.h>
```

```
void vcdiv (int n, double complex *y, int incy, const double complex *x, int incx, double complex a);
void vcdivf(int n, float complex *y, int incy, const float complex *x, int incx, float complex a);
```

Given an input vector  $\mathbf{x}$  and a scalar constant  $\alpha$  and a result vector  $\mathbf{y}$ , this function computes:

$$\mathbf{y} = \mathbf{x}/\alpha$$

**14.9.1 Parameters**

**N - INTEGER ENTRY:** Number of elements of  $\mathbf{x}$  and  $\mathbf{y}$ .

*CONSTRAINT:*  $n \geq 1$ .

**Y - ARRAY OF COMPLEX EXIT:** Result vector  $\mathbf{y}$ .

*CONSTRAINT:* Must contain  $n \times \text{incy}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{x}$ .

**INCY - INTEGER ENTRY:** Stride for the vector  $\mathbf{y}$ .

*CONSTRAINT:*  $\text{incy} > 0$ .

**X - ARRAY OF COMPLEX ENTRY:** Input vector  $\mathbf{x}$ .

*CONSTRAINT:* Must contain  $n \times \text{incx}$  elements.

*CONSTRAINT:* Must not overlap with array  $\mathbf{y}$ .

**INCX - INTEGER ENTRY:** Stride for the vector  $\mathbf{x}$ .

*CONSTRAINT:*  $\text{incx} > 0$ .

**A - COMPLEX ENTRY:** Scalar constant  $\alpha$ .

## 15 Acknowledgements

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 */
```

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