

**Compressible Flow Subroutine Library
Reference Manual (C/C++)
DD-00008-010**

Jan Adelsbach

January 26, 2024

Contents

1	About this Guide	5
1.1	Legal Information	5
1.2	Feedback and Contact	5
1.3	Introduction	5
1.4	Audience for This Guide	5
1.5	How to Use This Guide	5
1.6	Conventions Used in This Guide	5
2	Overview	6
2.1	Introduction	6
2.2	Performance Characteristics	6
2.3	Error Behavior	6
3	Function Reference	7
3.1	System functions	7
3.1.1	Introduction	7
3.1.2	arsyver - Get version information	8
3.1.3	arsyerr - Retrieve and reset error code	9
3.2	Characteristic Mach Number	10
3.2.1	Introduction	10
3.2.2	armcmm - Compute given normal mach number, M	11
3.2.3	armcms - Compute given characteristic mach number, M^*	12
3.3	Hugoniot compression	13
3.3.1	Introduction	13
3.3.2	arshud - Compute given density factor ρ_2/ρ_1	14
3.3.3	arshup - Compute given density factor p_2/p_1	15
3.4	Critical mach number	16
3.4.1	armcrm - Critical pressure coefficient given M_{crit}	17
3.4.2	armcrc - Critical mach number given C_p	18
3.4.3	armcrpg - Critical mach number given C_{p0} using Prandtl-Glauert pressure approximation	19
3.4.4	armcrla - Critical mach number given C_{p0} using Laitone pressure approximation	20
3.4.5	armcrkt - Critical mach number given C_{p0} using Karman-Tsien pressure approximation	21
3.5	Isentropic flow	22
3.5.1	Introduction	22
3.5.2	arfism - Isentropic relations given M	23
3.5.3	arfisp - Isentropic relations given p_2/p_1	24
3.5.4	arfisd - Isentropic relations given ρ_2/ρ_1	25
3.5.5	arfist - Isentropic relations given T_2/T_1	26
3.5.6	arfisa - Isentropic relations given A/A^*	27
3.6	Fanno flow	28
3.6.1	Introduction	28
3.6.2	arffam - Fanno relations given M	29
3.6.3	arffap - Fanno relations given p/p^*	30
3.6.4	arffad - Fanno relations given ρ/ρ^*	31
3.6.5	arffat - Fanno relations given T/T^*	32
3.6.6	arffav - Fanno relations given V/V^*	33
3.6.7	arffap0 - Fanno relations given p_{01}/p_{02}	34
3.6.8	arffaf - Fanno relations given $(4fL)/D$	35
3.6.9	arffads - Fanno relations given $(s - s^*)/c_p$	36
3.7	Rayleigh Flow	37
3.7.1	Introduction	37
3.7.2	arfram - Rayleigh relations given M	38
3.7.3	arfrap - Rayleigh relations given p/p^*	39
3.7.4	arfrad - Rayleigh relations given ρ/ρ^*	40
3.7.5	arfrat - Rayleigh relations given T/T^*	41
3.7.6	arfrav - Rayleigh relations given V/V^*	42
3.7.7	arfrap0 - Rayleigh relations given p_{02}/p_{01}	43

3.7.8 arfrat0 - Rayleigh relations given T_{02}/T_{01} 44

3.7.9 arfrads - Rayleigh relations given $(s - s^*)/c_p$ 45

3.8 Isothermal flow through long duct 46

3.8.1 Introduction 46

3.8.2 arfitm - Isothermal relations given M 47

3.8.3 arfitv - Isothermal relations given V/V^* 48

3.8.4 arfits - Isothermal relations given $p^*/p, r^*/r, M^*/M$ 49

3.8.5 arfitp0 - Isothermal relations given p_{01}/p_{02} 50

3.8.6 arfitt0 - Isothermal relations given T_{02}/T_{01} 51

3.8.7 arfitf - Isothermal relations given $(4fL)/D$ 52

3.9 DeLaval nozzle flow 53

3.9.1 Introduction 53

3.9.2 arfqism - DeLaval isentropic flow relations given M 54

3.9.3 arfqisp - DeLaval isentropic flow relations given p/p_1 55

3.9.4 arfqisd - DeLaval isentropic flow relations given ρ/ρ_1 56

3.9.5 arfqist - DeLaval isentropic flow relations given T/T_1 57

3.9.6 arfqisa - DeLaval isentropic flow relations given A/A^* 58

3.10 Normal Shock Waves 59

3.10.1 Introduction 59

3.10.2 arsnsm1 - Normal shock relations given M_{1n} 60

3.10.3 arsnsm2 - Normal shock relations given M_{2n} 61

3.10.4 arsnsp - Normal shock relations given p_2/p_1 62

3.10.5 arnsnd - Normal shock relations given ρ_2/ρ_1 63

3.10.6 arsnst - Normal shock relations given T_2/T_1 64

3.10.7 arsnsp0 - Normal shock relations given p_{02}/p_{01} 65

3.11 Oblique Shock Relations 66

3.11.1 Introduction 66

3.11.2 arsolmw - Oblique shock relations given M_1 and δ 67

3.11.3 arsolpw - Oblique shock relations given p_2/p_1 and δ 68

3.11.4 arsoldw - Oblique shock relations given ρ_2/ρ_1 and δ 69

3.11.5 arsoltw - Oblique shock relations given T_2/T_1 and δ 70

3.11.6 arsolp0w - Oblique shock relations given p_{02}/p_{01} and δ 71

3.11.7 arsolws - Oblique shock relations given θ and δ 72

3.11.8 arsolms - Oblique shock relations given M_1 and θ 73

3.12 Oblique Shock Limits 74

3.12.1 Introduction 74

3.12.2 arsolld - Compute maximum wave and deflection surface angle before shock detachment 75

3.12.3 arsolls - Compute maximum wave and deflection surface angle that wil result in sonic down-stream flow 76

3.13 Prandtl-Meyer function 77

3.13.1 Introduction 77

3.13.2 arspmm - Prandtl-Meyer properties given M 78

3.13.3 arspmv - Prandtl-Meyer properties given $v(M)$ 79

3.13.4 arspmt - Prandtl-Meyer properties given θ 80

3.13.5 arspmfm - Prandtl-Meyer angle from M 81

3.13.6 arspmfv - Mach number from $v(M)$ 82

3.14 Expansion Fan (Rarefaction Wave) 83

3.14.1 Introduction 83

3.14.2 arsefm - Expansion fan properties given M_1 and M_2 84

3.14.3 arsefp - Expansion fan properties given p_2/p_1 and either M_1 or M_2 85

3.14.4 arsefd - Expansion fan properties given ρ_2/ρ_1 and either M_1 or M_2 86

3.14.5 arseft - Expansion fan properties given T_2/T_1 and either M_1 or M_2 87

3.15 (Rayleigh-)Pitot Tube Relations 88

3.15.1 Introduction 88

3.15.2 arspmt - (Rayleigh-)Pitot relations given M 89

3.15.3 arsppt - (Rayleigh-)Pitot relations given p_0/p or p_{02}/p_1 90

3.16 Reflected Shock Waves 91

3.16.1 Introduction 91

3.16.2 arsrms - Reflected shock wave mach number given M 92

3.16.3 arsrsmr - Incident shock wave mach number given M' 93

3.17 Quasi-2D Conical Flow 94

3.17.1 Introduction 94

3.17.2 arskomw - Conical flow given M and δ 95

3.17.3 arskomc - Conical flow given M and θ 96

3.18 Moving Normal Shock Waves 97

3.19 Moving Normal Shock Waves (Thermodynamic Properties) 97

3.19.1 Introduction 97

3.19.2 arsmnsm - Moving shock relations given M 98

3.19.3 arsmnsp - Moving shock relations given p_2/p_1 99

3.19.4 arsmnsd - Moving shock relations given ρ_2/ρ_1 100

3.19.5 arsmnst - Moving shock relations given T_2/T_1 101

3.20 Moving Normal Shock Waves (Dynamic Properties) 102

3.20.1 Introduction 102

3.20.2 arsmnvp - Dynamic moving shock relations given p_2/p_1 103

3.20.3 arsmnvw - Dynamic moving shock relations given V 104

3.20.4 arsmnvup - Dynamic moving shock relations given U_p 105

3.21 Karman-Tsien Pressure Correction Coefficient 106

3.21.1 Introduction 106

3.21.2 arckarcp - Karman-Tsien pressure correction given M and C_{p0} 107

3.21.3 arckarci - Karman-Tsien pressure correction given M and C_p 108

3.22 Laitone Pressure Correction Coefficient 109

3.22.1 Introduction 109

3.22.2 arclai cp - Laitone pressure correction given M and C_{p0} 110

3.22.3 arclai ci - Laitone pressure correction given M and C_p 111

3.23 Prandtl-Glauert Pressure Correction Coefficient 112

3.23.1 Introduction 112

3.23.2 arcp gl cp - Prandtl-Glauert pressure correction given M and C_{p0} 113

3.23.3 arcp gl ci - Prandtl-Glauert pressure correction given M and C_p 114

1 About this Guide

1.1 Legal Information

Copyright ©2024 Adelsbach UG (haftungsbeschränkt). All Rights Reserved.

Copyright ©2016-2024 Jan Adelsbach. All Rights Reserved.

From herein referred to as *Adelsbach*.

This document may not be reproduced without written permission by Adelsbach.

1.2 Feedback and Contact

For feedback on this document, please use the following email address:

techpubs@adelsbach-research.eu

Please include the page number or a link to the page.

For general contact details, please visit <https://adelsbach-research.eu/contact>.

1.3 Introduction

This manual describes the *Application Programming Interface* (API) of the *Compressible Flow Subroutine Library* for the C and C++ programming language families.

1.4 Audience for This Guide

The audience of this guide is assumed to be C or C++ programmers who understand the basic concepts of at least one of the aforementioned programming languages.

Familiarity with pointer based arrays in C/C++ is strongly recommended.

1.5 How to Use This Guide

This guide first describes some general programming details of the library and then documents each function individually.

1.6 Conventions Used in This Guide

x

Normal math typesetting represents a normal variable.

x

Bold math typesetting represents a vector.

Mono

Monospace typesetting represents C function names, variables or data types.

2 Overview

2.1 Introduction

2.2 Performance Characteristics

Each function or subroutine has a declared performance characteristic, these represent how the performance of a function can be predicted.

Fixed The function always executes around the same amount of instructions. Depending upon the actual values passed in the arguments there might be insignificant variations but do not contain any iterative solver. The behavior of standard library functions used is not considered for this performance classification.

Iterative The function uses an iterative root finding algorithm to compute the result. In the library all functions which use iterative solvers have a maximum amount of iterations, after which they will fail.

Iterative solvers are usually non-linear root finding methods such as Newton-Raphson, False Position or Bisection style solvers or can be solvers for differential equations such as Runge-Kutta methods as described in [DKahaner1988].

2.3 Error Behavior

All library subroutines where an error may occur usually have an optional integer pointer argument. If the latter is given and an error occurs the error code will be written into the integer at the pointer's location. If no error occurs the integer will not be changed. As such this allows by design a logical-OR behavior in which one may call several subroutines and check at the very end whether an error code has been set.

This error code is also set into a *thread-local* variable and can be inquired using the 3.1.3 function for the current thread. The latter will also provide the name of the offending function for easier traceback.

Functions that are designed for specific purposes may however return NaN (*Not-a-Number*) or infinity ∞ . The specific error behavior for those is documented for each of such functions individually.

3 Function Reference

3.1 System functions

3.1.1 Introduction

The functions in this group provide system information about the CFSL library and error handling facilities.

3.1.2 arsyver - Get version information

```
void arsyver(short *major, short *minor, const char **cmplr);
```

Return the major, minor version and the compiler used to compile the library.

Arguments

Argument	Intent	Description
major	out	(<i>optional</i>) Pointer to store major version in
minor	out	(<i>optional</i>) Pointer to store minor version in
cmplr	out	(<i>optional</i>) Pointer to store a pointer to the compiler version string

3.1.3 arsyerr - Retrieve and reset error code

```
int arsyerr(const char **fn, bool clear);
```

Returns the last error code and messages that occurred in the current thread.

Parameters

Argument	Intent	Description
fn	out	(<i>optional</i>) Pointer to store a pointer to the function name string
clear	in	Whether to clear the error code from the <i>thread-local</i> context

3.2 Characteristic Mach Number

3.2.1 Introduction

This function group computes the characteristic Mach Number M^* as given in [JDAnderson1982] and [Shapiro1953] from a given mach number M or in reverse the latter given M^* . The characteristic mach number has the following properties:

$$\begin{aligned} M^* &= 0 && \text{if } M = 0 \\ M^* &= 1 && \text{if } M = 1 \\ M^* &< 1 && \text{if } M < 1 \\ M^* &> 1 && \text{if } M > 1 \end{aligned}$$

And furthermore the its most useful property:

$$\lim_{M \rightarrow \infty} M^* = \sqrt{\frac{\gamma + 1}{\gamma - 1}}$$

The following properties are computed:

Table 1: Characteristic mach number properties

I	Symbol	Description
1	M	Mach number
2	M^*	Characteristic mach number

3.2.2 armcmm - Compute given normal mach number, M

```
double armcmm(double g, double m, int *ierr)
```

Compute given normal mach number, M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ
m	in	Mach number $M > 0$
ierr	out	(optional) Return status code

Status Codes

-1 Specific heat ratio $\gamma \leq 1$.

-2 Given $M \leq 0$.

Return Value

Characteristic mach number M^* or NAN on error.

3.2.3 armcms - Compute given characteristic mach number, M^*

```
double armcms(double g, double mstar, int *ierr)
```

Compute given the characteristic mach number, M^* . Note that if $M^* = \sqrt{(\gamma+1)(\gamma-1)}$ the function will return $M = \infty = \text{INFINITY}$.

Performance

Fixed

Parameters

Argument	Intent	Description
g	in	Specific heat constant γ
mstar	in	Characteristic mach number $0 < M^* \leq \sqrt{(\gamma+1)(\gamma-1)}$.
ierr	out	(optional) Return status code

Status Codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 3 Given M^* out of specified range.

Return Value

Normal mach number M or NAN on error.

3.3 Hugoniot compression

3.3.1 Introduction

Hugoniot's equation can be used to model a normal shock wave by thermodynamic constants only as given by [JAnderson1982]. As such this equation allows the relation of the pressure factor over the shock wave p_2/p_1 to the density factor over the same ρ_2/ρ_1 given a specific heat constant γ without being related to a velocity or mach number. Note that the Hugoniot based shock wave compression does not yield exactly the same results as normal shock wave relations and in fact deviates from them at higher mach numbers. The following properties are computed:

Table 2: Hugoniot compression properties

I	Symbol	Description
1	p_2/p_1	Pressure factor
2	ρ_2/ρ_1	Density factor

3.3.2 arshud - Compute given density factor ρ_2/ρ_1

```
double arshud(double g, double d, int *ierr);
```

Compute pressure factor based upon density factor ρ_2/ρ_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density fraction $0 < \rho_2/\rho_1 < \sqrt{\frac{\gamma+1}{\gamma-2}}$.
ierr	out	(<i>optional</i>) Return status code.

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given ρ_2/ρ_1 out of range.

Return Value

Pressure fraction p_2/p_1 or NAN on error.

3.3.3 arshup - Compute given density factor p_2/p_1

```
double arshup(double g, double p, int *ierr);
```

Compute pressure factor based upon pressure factor p_2/p_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure fraction $p_2/p_1 > 0$.
ierr	out	(optional) Return status code.

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given p_2/p_1 out of range.

Return Value

Density fraction ρ_2/ρ_1 or NAN on error.

3.4 Critical mach number

3.4.1 armcrm - Critical pressure coefficient given M_{crit}

```
double armcrm(double g, double mcrit, int *ierr);
```

Compute given the critical pressure coefficient given M_{crit} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
mcrit	in	Critical Mach number $0 < M_{\text{crit}} < 1$.
ierr	out	(optional) Return status code

Status codes

-1 Specific heat ratio $\gamma \leq 1$.

-2 Given M_{crit} out of range.

Return Value

Critical pressure coefficient C_p or NAN on error.

3.4.2 armcrc - Critical mach number given C_p

```
double armcrc(double g, double cp, int *ierr);
```

Compute given the critical mach number given C_p .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
cp	in	Critical pressure coefficient C_p .
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given C_p out of range.
- 3 Iterative solver failed.

Return Value

Critical mach number M_{crit} or NAN on error.

3.4.3 armcrpg - Critical mach number given C_{p0} using Prandtl-Glauert pressure approximation

```
double armcrpg(double g, double cp0, int *ierr);
```

Compute critical mach number given C_{p0} Prandtl-Glauert pressure approximation.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
cp0	in	Critical pressure coefficient C_{p0} .
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Iterative solver failed.

Return Value

Critical mach number M_{crit} or NAN on error.

3.4.4 armcrla - Critical mach number given C_{p0} using Laitone pressure approximation

```
double armcrla(double g, double cp0, int *ierr);
```

Compute critical mach number given C_{p0} Laitone pressure approximation.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
cp0	in	Critical pressure coefficient C_{p0} .
ierr	out	(optional) Return status code

Status codes

-1 Specific heat ratio $\gamma \leq 1$.

-2 Iterative solver failed.

Return Value

Critical mach number M_{crit} or NAN on error.

3.4.5 armcrkt - Critical mach number given C_{p0} using Karman-Tsien pressure approximation

```
double armcrkt(double g, double cp0, int *ierr);
```

Compute critical mach number given C_{p0} Karman-Tsien pressure approximation.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
cp0	in	Critical pressure coefficient C_{p0} .
ierr	out	(optional) Return status code

Status codes

-1 Specific heat ratio $\gamma \leq 1$.

-2 Iterative solver failed.

Return Value

Critical mach number M_{crit} or NAN on error.

3.5 Isentropic flow

3.5.1 Introduction

This function group computes the thermodynamic properties of isentropic flow for a calorically perfect gas as described in [naca1135] with one-dimensional variable changes. Isentropic flow assumes the following continuity equation:

$$\rho AV = \text{const}$$

The momentum equation is:

$$p + \rho AV^2 = \text{const}$$

The following properties are computed:

Table 3: Isentropic flow properties

I	Property	Description
1	M	Mach number
2	p_0/p_1	Pressure ratio
3	ρ_0/ρ_1	Density ratio
4	T_0/T_1	Temperature ratio
5	A/A^*	Critical area ratio

3.5.2 arfism - Isentropic relations given M

```
void arfism(double g, double m, double result[5], int *ierr);
```

Compute the isentropic relations given the mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 3.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.5.3 arfisp - Isentropic relations given p_2/p_1

```
void arfisp(double g, double p, double result[5], int *ierr);
```

Compute the isentropic relations given the pressure ratio p_2/p_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $0 \leq p_2/p_1 \leq 1$.
result	out	Array with result properties as described in 3.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p_2/p_1 out of range.

3.5.4 arfisd - Isentropic relations given ρ_2/ρ_1

```
void arfisd(double g, double r, double result[5], int *ierr);
```

Compute the isentropic relations given the density ratio ρ_2/ρ_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
r	in	Density ratio $0 \leq \rho_2/\rho_1 \leq 1$.
result	out	Array with result properties as described in 3.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given ρ_2/ρ_1 out of range.

3.5.5 arfist - Isentropic relations given T_2/T_1

```
void arfist(double g, double t, double result[5], int *ierr);
```

Compute the isentropic relations given the temperature ratio T_2/T_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Temperature ratio $0 \leq T_2/T_1 \leq 1$.
result	out	Array with result properties as described in 3.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given T_2/T_1 out of range.

3.5.6 arfisa - Isentropic relations given A/A^*

```
void arfisa(double g, double a, bool is_sub, double result[5], int *ierr);
```

Compute the isentropic relations given the critical area ratio A/A^* .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
a	in	Critical area ratio $A/A^* \geq 1$.
is_sub	in	Whether the mach number corresponding to A/A^* is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 3.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given A/A^* out of range.
- 4 Iterative solver failed

3.6 Fanno flow

3.6.1 Introduction

This function group computes the thermodynamic properties of adiabatic flow with friction for calorically perfect gas as described in [JAnderson1982].

The following properties are computed:

Table 4: Fanno flow properties

I	Property	Description
1	M	Mach number
2	p/p^*	Pressure ratio
3	ρ/ρ^*	Density ratio
4	T/T^*	Temperature ratio
5	V/V^*	Velocity ratio
6	p_{01}/p_{02}	Stagnation pressure ratio
7	$(4fL)/D$	Fanno line
8	$(s - s^*)/c_p$	Change in entropy

3.6.2 arffam - Fanno relations given M

```
void arffam(double g, double m, double result[8], int *ierr);
```

Description

Compute the fanno relations given a mach number, M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 4.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.6.3 arffap - Fanno relations given p/p^*

```
void arffap(double g, double p, double result[8], int *ierr);
```

Compute the fanno relations given the pressure ratio, p/p^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $0 \leq p/p^*$.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p/p^* out of range.

3.6.4 arffad - Fanno relations given ρ/ρ^*

```
void arffad(double g, double d, double result[8], int *ierr);
```

Compute the fanno relations given the density ratio, ρ/ρ^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $\sqrt{(\gamma - 1)/(\gamma + 1)} \leq \rho/\rho^*$.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given ρ/ρ^* out of range.

3.6.5 arffat - Fanno relations given T/T^*

```
void arffat(double g, double t, double result[8], int *ierr);
```

Compute the fanno relations given the temperature ratio, T/T^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Temperature ratio $0 \leq T/T^* \leq (\gamma + 1)/(\gamma - 1)$.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given T/T^* out of range.

3.6.6 arffav - Fanno relations given V/V^*

```
void arffav(double g, double v, double result[8], int *ierr);
```

Compute the fanno relations given the velocity ratio, V/V^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
v	in	Velocity ratio $0 \leq V/V^* \leq \sqrt{(\gamma + 1)/(\gamma - 1)}$.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given V/V^* out of range.

3.6.7 arffap0 - Fanno relations given p_{01}/p_{02}

```
void arffap0(double g, double p0, bool is_sub, double result[8], int *ierr);
```

Compute the fanno relations given the stagnation pressure ratio, p_{01}/p_{02} .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p0	in	Stagnation pressure ratio $1 \leq p_{02}/p_{01}$.
is_sub	in	Whether M corresponding to the given p_{02}/p_{01} is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 4.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p_{01}/p_{02} out of range.
- 4 Iterative solver failed.

3.6.8 arffaf - Fanno relations given $(4fL)/D$

```
void arffaf(double g, double l, bool is_sub, double result[8], int *ierr);
```

Compute the fanno relations given the fanno line, $(4fL)/D$.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
l	in	Fanno line $0 \leq (4fL)/D \leq ((\gamma + 1)\log((\gamma + 1)/(\gamma - 1)) - 2)/(2\gamma)$.
is_sub	in	Whether M corresponding to the given $(4fL)/D$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given $(4fL)/D$ out of range.
- 4 Iterative solver failed.

3.6.9 arffads - Fanno relations given $(s - s^*)/c_p$

```
void arffads(double g, double ds, bool is_sub, double result[8], int *ierr);
```

Compute the fanno relations given the fanno line, $(s - s^*)/c_p$.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
ds	in	Change in entropy $-\infty < (s - s^*)/c_p < \infty$.
is_sub	in	Whether M corresponding to the given $(s - s^*)/c_p$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given $(s - s^*)/c_p$ out of range.
- 4 Iterative solver failed.

3.7 Rayleigh Flow

3.7.1 Introduction

This function group computes the thermodynamic properties of non-adiabatic flow with heat addition for a calorically perfect gas as described in [JDAnderson1982].

The computed properties are as follows:

Table 5: Rayleigh flow properties

I	Property	Description
1	M	Mach number
2	p/p^*	Pressure ratio
3	ρ/ρ^*	Density ratio
4	T/T^*	Temperature ratio
5	V/V^*	Velocity ratio
6	p_{01}/p_{02}	Stagnation pressure ratio
7	T_{01}/T_{02}	Stagnation temperature ratio
8	$(s - s^*)/c_p$	Change in entropy

3.7.2 arfram - Rayleigh relations given M

```
void arfram(double g, double m, double result[8], int *ierr);
```

Compute the rayleigh relations given a mach number, M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 5.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.7.3 arfrac - Rayleigh relations given p/p^*

```
void arfrac(double g, double p, double result[8], int *ierr);
```

Compute the rayleigh relations given the pressure ratio, p/p^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $0 < p/p^* < \gamma + 1$.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p/p^* out of range.

3.7.4 arfrac - Rayleigh relations given ρ/ρ^*

```
void arfrac(double g, double d, double result[8], int *ierr);
```

Compute the rayleigh relations given the density ratio, ρ/ρ^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $\gamma(\gamma + 1) < \rho/\rho^*$.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given ρ/ρ^* out of range.

3.7.5 arfrac - Rayleigh relations given T/T^*

```
void arfrac(double g, double t, bool tmax, double result[8], int *ierr);
```

Compute the rayleigh relations given the temperature ratio, T/T^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Temperature ratio $0 < T/T^*$.
tmax	in	Whether the static temperature ratio supplied is for a low speed false or a high speed true.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given T/T^* out of range.

3.7.6 arfrac - Rayleigh relations given V/V^*

```
void arfrac(double g, double v, double result[8], int *ierr);
```

Compute the rayleigh relations given the velocity ratio, V/V^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
v	in	Velocity ratio $0 < V/V^* < (\gamma + 1)/\gamma$.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given V/V^* out of range.

3.7.7 arfrap0 - Rayleigh relations given p_{02}/p_{01}

```
void arfrap0(double g, double p0, bool is_sub, double result[8], int *ierr);
```

Compute the rayleigh relations given the stagnation pressure ratio, p_{02}/p_{01} .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p0	in	Stagnation pressure ratio $p_{02}/p_{01} > \frac{\gamma^2-1}{\gamma^2}$.
is_sub	in	Whether M corresponding to the given p_{02}/p_{01} is assumed to be sub- or super-sonic.
result	out	Array with result properties as described in 5.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p_{02}/p_{01} out of range.
- 4 Iterative solver failed.

3.7.8 arfrat0 - Rayleigh relations given T_{02}/T_{01}

```
void arfrat0(double g, double t0, bool is_sub, double result[8], int *ierr);
```

Compute the rayleigh relations given the stagnation temperature ratio, T_{02}/T_{01} .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t0	in	Stagnation temperature ratio $T_{02}/T_{01} \geq 0$.
is_sub	in	Whether M corresponding to the given T_{02}/T_{01} is assumed to be sub- or super-sonic.
result	out	Array with result properties as described in 5.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given T_{02}/T_{01} out of range.
- 4 Iterative solver failed.

3.7.9 arfrads - Rayleigh relations given $(s - s^*)/c_p$

```
void arfrads(double g, double ds, bool is_sub, double result[8], int *ierr);
```

Compute the rayleigh relations given the fanno line, $(s - s^*)/c_p$.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
ds	in	Change in entropy $-\infty < (s - s^*)/c_p < \infty$.
is_sub	in	Whether M corresponding to the given $(s - s^*)/c_p$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given $(s - s^*)/c_p$ out of range.
- 4 Iterative solver failed.

3.8 Isothermal flow through long duct

3.8.1 Introduction

This function group computes an isothermal flow through a long ducts as described in [VLStreeter1966] for which neither fanno nor rayleigh flow is applicable due to the assumptions of the two latter.

The following properties are computed:

Table 6: Isothermal flow properties

I	Property	Description
1	M	Mach number
2	$\frac{p^*}{p}, \frac{r^*}{r}, \frac{M^*}{M}$	Non-stagnative ratios
3	ρ/ρ^*	Density ratio
5	V/V^*	Velocity ratio
6	p_{01}/p_{02}	Stagnation pressure ratio
6	T_{01}/T_{02}	Stagnation temperature ratio
7	$(4fL)/D$	Characteristic line

3.8.2 arfitm - Isothermal relations given M

```
void arfitm(double g, double m, double result[6], int *ierr);
```

Compute the isothermal relations given the mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.8.3 arfitv - Isothermal relations given V/V^*

```
void arfitv(double g, double v, double result[6], int *ierr);
```

Compute the isothermal relations given the velocity ratio, V/V^* .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
v	in	Velocity ratio $V/V^* > 0$.
result	out	Array with result properties as described in 6.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given V/V^* out of range.

3.8.4 arfits - Isothermal relations given $p^*/p, r^*/r, M^*/M$

```
void arfits(double g, double s, double result[6], int *ierr);
```

Compute the isothermal relations given a non-stagnative ratio, $p^*/p, r^*/r, M^*/M$.

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
s	in	Non-stagnative ratio $p^*/p, r^*/r, M^*/M > 0$.
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given non-stagnative ratio out of range.

3.8.5 arfitp0 - Isothermal relations given p_{01}/p_{02}

```
void arfitp0(double g, double p0, bool is_sub, double result[6], int *ierr);
```

Compute the isothermal relations given the stagnation pressure ratio, p_{01}/p_{02} .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p0	in	Stagnation pressure ratio $1 \leq p_{02}/p_{01}$.
is_sub	in	Whether M corresponding to the given p_{02}/p_{01} is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p_{01}/p_{02} out of range.
- 4 Iterative solver failed.

3.8.6 arfitt0 - Isothermal relations given T_{02}/T_{01}

```
void arfitt0(double g, double t0, double result[6], int *ierr);
```

Compute the isothermal relations given the stagnation temperature T_{02}/T_{01} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t0	in	Stagnation temperature $T_{02}/T_{01} > 0$.
result	out	Array with result properties as described in 6.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given T_{02}/T_{01} out of range.

3.8.7 arfitf - Isothermal relations given $(4fL)/D$

```
void arfitf(double g, double l, bool is_sub, double result[6], int *ierr);
```

Compute the isothermal relations given the characteristic line, $(4fL)/D$.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
l	in	Characteristic line $(4fL)/D$.
is_sub	in	Whether M corresponding to the given $(4fL)/D$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given $(4fL)/D$ out of range.
- 4 Iterative solver failed.

3.9 DeLaval nozzle flow

3.9.1 Introduction

This function group computes the properties of *quasi-2D* isentropic flow through a DeLaval nozzle, as described in [JDAnderson1982].

The following properties are computed:

Table 7: DeLaval nozzle properties

I	Property	Description
1	M	Mach number
2	p/p_1	Pressure ratio
3	ρ/ρ^*	Density ratio
4	T/T_1	Temperature ratio
5	A/A_1	Critical area ratio

3.9.2 arfqism - DeLaval isentropic flow relations given M

```
void arfqism(double g, double m, double result[5], int *ierr);
```

Compute the DeLaval nozzle isentropic relations given the mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.9.3 arfqisp - DeLaval isentropic flow relations given p/p_1

```
void arfqisp(double g, double p, double result[5], int *ierr);
```

Compute the DeLaval nozzle isentropic relations given the pressure ratio p/p_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $0 < p/p_1 < 1$.
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p/p_1 out of range.

3.9.4 arfqisd - DeLaval isentropic flow relations given ρ/ρ_1

```
void arfqisd(double g, double d, double result[5], int *ierr);
```

Compute the DeLaval nozzle isentropic relations given the density ratio p/p_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $0 < \rho/\rho_1 < 1$.
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given ρ/ρ_1 out of range.

3.9.5 arfqist - DeLaval isentropic flow relations given T/T_1

```
void arfqist(double g, double t, double result[5], int *ierr);
```

Compute the DeLaval nozzle isentropic relations given the temperature ratio T/T_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $0 < T/T_1 < 1$.
result	out	Array with result properties as described in 7.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given T/T_1 out of range.

3.9.6 arfqisa - DeLaval isentropic flow relations given A/A^*

```
void arfqisa(double g, double a, bool is_sub, double result[5], int *ierr);
```

Compute the DeLaval nozzle isentropic relations given the critical area ratio A/A^* .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
a	in	Critical area ratio $A/A^* > 1$.
is_sub	in	Whether the mach number corresponding to A/A^* is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given A/A^* out of range.
- 4 Iterative solver failed.

3.10 Normal Shock Waves

3.10.1 Introduction

These functions compute the thermodynamic properties across a normal shock wave, assuming a calorically perfect gas and an adiabatic and frictionless flow, as described in [naca1135]. It can compute the following set of properties given one of the properties in conjunction with a specific heat ratio γ of the gas medium.

The following equations govern normal shock waves as implemented in the function group:

Equation of Mass

$$p_1 u_1 = p_2 u_2$$

Equation of Momentum

$$p_1 + \rho_1 u_1^2 = p_2 + \rho_2 u_2^2$$

Equation of Energy

$$\frac{1}{2} u_1^2 + h_1 = \frac{1}{2} u_2^2 + h_2 \text{ [adiab]}$$

Normal Shock Waves are classified by the following properties, where the subscript 1,2 refers to upstream and downstream, respectively.

The following properties are computed:

Table 8: Normal shock properties

I	Property	Description
1	M_{1n}	Upstream mach number
2	M_{2n}	Downstream mach number
3	p_2/p_1	Pressure ratio
4	ρ_2/ρ_1	Density ratio
5	T_2/T_1	Temperature ratio
6	p_{02}/p_{01}	Stagnation pressure ratio

3.10.2 arsnsm1 - Normal shock relations given M_{1n}

```
void arsnsm1(double g, double m, double result[5], int *ierr);
```

Compute the normal shock relations given the upstream mach number M_{1n} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Upstream number $M_{1n} \geq 1$.
result	out	Array with result properties as described in 8.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_{1n} out of range.

3.10.3 arsnsm2 - Normal shock relations given M_{2n}

```
void arsnsm2(double g, double m, double result[5], int *ierr);
```

Compute the normal shock relations given the downstream mach number M_{2n} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Upstream number $M_{2n} > 0$.
result	out	Array with result properties as described in 8.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_{2n} out of range.

3.10.4 arsnsp - Normal shock relations given p_2/p_1

```
void arsnsp(double g, double p, double result[5], int *ierr);
```

Compute the normal shock relations given the pressure ratio p_2/p_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $p_2/p_1 < 1$.
result	out	Array with result properties as described in 8.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M_{1n} out of range.
- 3 Given p_2/p_1 out of range.

3.10.5 arsnsd - Normal shock relations given ρ_2/ρ_1

```
void arsnsd(double g, double d, double result[5], int *ierr);
```

Compute the normal shock relations given the density ratio ρ_2/ρ_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $1 \leq \rho_2/\rho_1 \leq (\gamma + 1)/(\gamma - 1)$.
result	out	Array with result properties as described in 8.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M_{1n} out of range.
- 3 Given ρ_2/ρ_1 out of range.

3.10.6 arsnst - Normal shock relations given T_2/T_1

```
void arsnst(double g, double t, double result[5], int *ierr);
```

Compute the normal shock relations given the temperature ratio T_2/T_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Temperature ratio $T_2/T_1 \geq 1$.
result	out	Array with result properties as described in 8.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M_{1n} out of range.
- 3 Given T_2/T_1 out of range.

3.10.7 arsnsp0 - Normal shock relations given p_{02}/p_{01}

```
void arsnsp0(double g, double p0, double result[5], int *ierr);
```

Compute the normal shock relations given the stagnation pressure ratio p_{02}/p_{01} .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p0	in	Stagnation pressure ratio $0 \leq p_{02}/p_{01} \leq 1$.
result	out	Array with result properties as described in 8.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M_{1n} out of range.
- 3 Given p_{02}/p_{01} out of range.
- 4 Iterative solver failed.

3.11 Oblique Shock Relations

3.11.1 Introduction

This function group computes the thermodynamic properties of an oblique shock wave given either a mach number and the surface deflection or wave angle or based upon both the wave and deflection surface angles, using algorithms as described in [usafv1], [naca1135] and [NASA187173].

Oblique Shock Waves are classified by the following properties, where the subscript 1,2 refers to upstream and downstream, respectively. The normal mach numbers M_{1n} and M_{2n} represent the mach numbers through the shock front as by the normal shock wave equations.

The following properties will be available:

Table 9: Oblique shock properties

I	Property	Description
1	M_1	Upstream mach number
2	M_2	Downstream mach number
3	M_{1n}	Normal upstream mach number
4	M_{2n}	Normal downstream mach number
5	θ	Deflection surface angle (°)
6	δ	Wave angle (°)
7	p_2/p_1	Pressure ratio
8	ρ_2/ρ_1	Density ratio
9	T_2/T_1	Temperature ratio
10	p_{02}/p_{01}	Stagnation pressure ratio

3.11.2 arsolmw - Oblique shock relations given M_1 and δ

```
void arsolmw(double g, double m, double d, double result[10], int *ierr);
```

Compute the oblique shock relations given a mach number M and the wave angle δ .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M_1 \geq 1$.
d	in	Wave angle $0 < \delta < 90$.
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_1 out of range.
- 3 Given δ out of range.

3.11.3 arsolpw - Oblique shock relations given p_2/p_1 and δ

```
void arsolpw(double g, double p, double d, double result[10], int *ierr);
```

Compute the oblique shock relations given the pressure ratio p_2/p_1 and the wave angle δ .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $p_2/p_1 > -(\gamma - 1)/(\gamma + 1)$.
d	in	Wave angle $0 < \delta < 90$.
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given p_2/p_1 out of range.
- 3 Given δ out of range.

3.11.4 `arsoldw` - Oblique shock relations given ρ_2/ρ_1 and δ

```
void arsoldw(double g, double ds, double d, double result[10], int *ierr);
```

Compute the oblique shock relations given the density ratio ρ_2/ρ_1 and the wave angle δ .

Performance

Fixed

Arguments

Argument	Intent	Description
<code>g</code>	in	Specific heat constant γ .
<code>p</code>	in	Density ratio $0 < \rho_2/\rho_1 < (\gamma + 1)/(\gamma - 1)$.
<code>d</code>	in	Wave angle $0 < \delta < 90$.
<code>result</code>	out	Array with result properties as described in 9.
<code>ierr</code>	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given ρ_2/ρ_1 out of range.
- 3 Given δ out of range.

3.11.5 `arsoltw` - Oblique shock relations given T_2/T_1 and δ

```
void arsoltw(double g, double t, double d, double result[10], int *ierr);
```

Compute the oblique shock relations given the temperature ratio T_2/T_1 and the wave angle δ .

Performance

Fixed

Arguments

Argument	Intent	Description
<code>g</code>	in	Specific heat constant γ .
<code>t</code>	in	Temperature ratio T_2/T_1 .
<code>d</code>	in	Wave angle $0 < \delta < 90$.
<code>result</code>	out	Array with result properties as described in 9.
<code>ierr</code>	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given T_2/T_1 out of range.
- 3 Given δ out of range.

3.11.6 arsolp0w - Oblique shock relations given p_{02}/p_{01} and δ

```
void arsolp0w(double g, double p0, double d, double result[10], int *ierr);
```

Compute the oblique shock relations given the stagnation pressure p_{02}/p_{01} and the wave angle δ .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p0	in	Stagnation pressure ratio p_{02}/p_{01} .
d	in	Wave angle $0 < \delta < 90$.
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given p_{02}/p_{01} out of range.
- 3 Given δ out of range.
- 4 Iterative solver failed.

3.11.7 arsolws - Oblique shock relations given θ and δ

```
void arsolws(double g, double d, double t, double result[10], int *ierr);
```

Compute the oblique shock relations given the deflection surface angle θ and the wave angle δ .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Deflection surface angle $0 < \theta < 90$.
d	in	Wave angle $0 < \delta < 90$.
result	out	Array with result properties as described in 9.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 3 Given θ or δ out of range.

3.11.8 arsolms - Oblique shock relations given M_1 and θ

```
void arsolms(double g, double m, double t, bool strong, double result[10], int *ierr);
```

Compute the oblique shock relations given the mach number M_1 and the deflection surface angle θ .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $M_1 \geq 1$.
t	in	Deflection surface angle $0 < \theta < 90$.
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_1 out of range.
- 3 Given θ out of range.
- 4 Calculation failed.

3.12 Oblique Shock Limits

3.12.1 Introduction

This set of functions computes the angle limits where an oblique shock would become detached or where the downstream flow would become sonic.

The following properties are computed:

Table 10: Oblique limit properties

I	Property	Description
1	M	Mach number for which the limit applies.
2	δ_{\max}	Maximum wave angle ($^{\circ}$).
3	θ_{\max}	Maximum deflection surface angle ($^{\circ}$).

3.12.2 arsolld - Compute maximum wave and deflection surface angle before shock detachment

```
void arsolld(double g, double m, double result[3], int *ierr);
```

Compute maximum wave and deflection surface angle before shock detachment given a mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M \geq 1$.
result	out	Array with result properties as described in 10.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.12.3 arsolls - Compute maximum wave and deflection surface angle that wil result in sonic downstream flow

```
void arsolls(double g, double m, double result[3], int *ierr);
```

Compute maximum wave and deflection surface angle that wil result in sonic downstream flow given a mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M \geq 1$.
result	out	Array with result properties as described in 10.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.13 Prandtl-Meyer function

3.13.1 Introduction

This function group contains a forward and inverse Prandtl-Meyer function, these two functions are separated from the expansion fan and normal shock function groups for convenience. The properties computed are as follows:

Table 11: Prandtl-Meyer properties

I	Property	Description
1	M	Mach number.
2	$v(M)$	Prandtl-Meyer function (°).
3	θ	Mach angle (°).

3.13.2 arspmm - Prandtl-Meyer properties given M

```
void arspmm(double g, double m, double result[3], int *ierr);
```

Compute the Prandtl-Meyer properties given a mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M \geq 1$.
result	out	Array with result properties as described in 11.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.13.3 arspmv - Prandtl-Meyer properties given $v(M)$

```
void arspmv(double g, double n, double result[3], int *ierr);
```

Compute the Prandtl-Meyer properties from the Prandtl-Meyer angle $v(M)$.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
n	in	Prandtl-Meyer angle $v(M) \leq 90 \left(\sqrt{\frac{\gamma+1}{\gamma-1}} - 1 \right)$.
result	out	Array with result properties as described in 11.
ierr	out	(<i>optional</i>) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 3 Given $v(M)$ out of range.
- 4 Iterative solver failed.

3.13.4 arspmt - Prandtl-Meyer properties given θ

```
void arspmt(double g, double t, double result[3], int *ierr);
```

Compute the Prandtl-Meyer properties given a mach angle θ .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Mach angle $0 \leq \theta \leq 90$.
result	out	Array with result properties as described in 11.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given θ out of range.

3.13.5 arspmfm - Prandtl-Meyer angle from M

```
double arspmfm(double g, double m);
```

Computes the Prandtl-Meyer angle $\nu(M)$ from the given mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M \geq 1$.

Return value

This function returns the Prandtl-Meyer angle $\nu(M)$ for the given mach number M or NAN (Not-a-Number) if an error has occurred).

3.13.6 arspmfv - Mach number from $v(M)$

```
double arspmfv(double g, double v);
```

Computes the mach number M given the Prandtl-Meyer angle $v(M)$.

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
n	in	Prandtl-Meyer angle $v(M) \leq 90 \left(\sqrt{\frac{\gamma+1}{\gamma-1}} - 1 \right)$.

Return value

This function returns the mach number M for the given mach Prandtl-Meyer angle $v(M)$ or NAN (Not-a-Number) if an error has occurred).

3.14 Expansion Fan (Rarefaction Wave)

3.14.1 Introduction

This class computes the thermodynamic properties of compressible gas flow over a wedge for a calorically perfect gas, as described by [naca1135]. It computes the following properties given the specific heat ratio γ and any of the up- or downstream mach number plus any of the other properties. After calling any of the evaluation functions the following properties will be available, where the subscript 1,2 refers to upstream and downstream, respectively;

The following properties are computed:

Table 12: Expansion fan properties

I	Property	Description
1	M_1	Upstream mach number.
2	M_2	Downstream mach number.
3	p_2/p_1	Pressure ratio.
4	ρ_2/ρ_1	Density ratio.
5	T_2/T_1	Temperature ratio.

3.14.2 arsefm - Expansion fan properties given M_1 and M_2

```
void arsefm(double g, double m1, double m2, double result[5], int *ierr);
```

Compute the expansion fan properties given M_1 and M_2 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m1	in	Upstream mach number $M_1 \geq 1$.
m2	in	Downstream mach number $M_2 > 0$.
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_1 or M_2 out of range.

3.14.3 arsefp - Expansion fan properties given p_2/p_1 and either M_1 or M_2

```
void arsefp(double g, double p, double m, bool is_m2, double result[5], int *ierr);
```

Compute the expansion fan properties given p_2/p_1 and either M_1 or M_2 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio p_2/p_1 .
m	in	Either $M_1 \geq 1$ or $M_2 > 0$ depending on whether is_m2 is false or true, respectively.
is_m2	in	Whether the given m refers to M_1 or M_2 .
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_1 or M_2 out of range.
- 3 Given pressure ratio p_2/p_1 out of range.

3.14.4 arsefd - Expansion fan properties given ρ_2/ρ_1 and either M_1 or M_2

```
void arsefd(double g, double d, double m, bool is_m2, double result[5], int *ierr);
```

Compute the expansion fan properties given ρ_2/ρ_1 and either M_1 or M_2 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio ρ_2/ρ_1 .
m	in	Either $M_1 \geq 1$ or $M_2 > 0$ depending on whether is_m2 is false or true, respectively.
is_m2	in	Whether the given m refers to M_1 or M_2 .
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_1 or M_2 out of range.
- 3 Given pressure ratio ρ_2/ρ_1 out of range.

3.14.5 arseft - Expansion fan properties given T_2/T_1 and either M_1 or M_2

```
void arseft(double g, double t, double m, bool is_m2, double result[5], int *ierr);
```

Compute the expansion fan properties given T_2/T_1 and either M_1 or M_2 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Temperature ratio T_2/T_1 .
m	in	Either $M_1 \geq 1$ or $M_2 > 0$ depending on whether is_m2 is false or true, respectively.
is_m2	in	Whether the given m refers to M_1 or M_2 .
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M_1 or M_2 out of range.
- 3 Given pressure ratio T_2/T_1 out of range.

3.15 (Rayleigh-)Pitot Tube Relations

3.15.1 Introduction

Computes the mach number out of the corresponding pressure given or inverse. For the supersonic case it computes the Rayleigh-Pitot equation which takes the bow shock in front of the pitot tube into account.

The following properties are computed: For $M < 1$ the Pitot pressure ratio p_0/p will be computed for $M \geq 1$ the

Table 13: (Rayleigh-)Pitot properties

I	Property	Description
1	M	Mach number.
2	p	Pressure ratio, see below

Rayleigh-Pitot pressure ratio p_{02}/p_1 will be computed.

3.15.2 arsptm - (Rayleigh-)Pitot relations given M

```
double arsptm(double g, double m, int *ierr);
```

Compute the Rayleigh-Pitot properties given a mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 13.
ierr	out	(optional) Return status code

Status codes

-1 Specific heat ratio $\gamma \leq 1$.

-2 Given M out of range.

Return Values

The pressure ratio p_0/p or p_{02}/p_1 or NAN on error.

3.15.3 arsptp - (Rayleigh-)Pitot relations given p_0/p or p_{02}/p_1

```
double arsptp(double g, double p0, bool is_sub, int *ierr);
```

Compute the Rayleigh-Pitot properties given a one of the pressure ratios p_0/p or p_{02}/p_1 .

Performance

- Fixed if `is_sub` is true.
- Iterative if `is_sub` is false.

Arguments

Argument	Intent	Description
<code>g</code>	in	Specific heat constant γ .
<code>p0</code>	in	The pressure ratio $p_0/p \geq 1$ or $p_{02}/p_1 \geq ((1+\gamma)/2)^{\gamma/(\gamma-1)}$ depending upon <code>is_sub</code> .
<code>is_sub</code>	in	Whether <code>p0</code> refers to a Pitot pressure fraction (true) or to a Rayleigh-Pitot pressure fraction (false).
<code>result</code>	out	Array with result properties as described in 13.
<code>ierr</code>	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given pressure ratio out of range.
- 3 Iterative solver failed.

Return Values

The Mach number M or NAN on error.

3.16 Reflected Shock Waves

3.16.1 Introduction

This function group computes the mach number of a reflected shock wave as given in [JDAnderson1982].

The following properties are computed:

Table 14: Reflected shock wave properties

I	Property	Description
1	M	Mach number of incident shock wave
2	M'	Mach number of reflected shock wave

3.16.2 arsrms - Reflected shock wave mach number given M

```
double arsrms(double g, double ms, int *ierr);
```

Computes the reflected shock wave mach number given M' .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
ms	in	Incident mach number $M \geq 1$.
result	out	Array with result properties as described in 14.
ierr	out	(optional) Return status code

Status codes

-1 Specific heat ratio $\gamma \leq 1$.

-2 Given M out of range.

Return values

The reflected shock wave mach number M' or NAN on error.

3.16.3 arsrsmr - Incident shock wave mach number given M'

```
double arsrsmr(double g, double mr, int *ierr);
```

Computes the incident shock wave mach number given M' .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Incident mach number $M' > 0$.
result	out	Array with result properties as described in 14.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M' out of range.
- 3 Iterative solver failed.

Return values

The incident shock wave mach number M or NAN on error.

3.17 Quasi-2D Conical Flow

3.17.1 Introduction

This function group computes a solution to the *Taylor-Maccoll* equation for axis symmetric flow around a cone as for example described in [JDAnderson1982], that is:

$$\frac{\gamma-1}{2} \left[1 - V_r'^2 - \left(\frac{dV_r'}{d\theta} \right)^2 \right] \left[2V_r' + \frac{dV_r'}{d\theta} \cot\theta + \frac{d^2V_r'}{d\theta^2} \right] - \frac{V_r'}{d\theta} \left[V_r' \frac{dV_r'}{d\theta} + \frac{dV_r'}{d\theta} \frac{d^2V_r'}{d\theta^2} \right] = 0$$

The solution to the above can be found given any combination of: the deflection surface angle θ of the cone, an approximated wave angle δ (i.e. using oblique shock relations) and the upstream mach number M . The solution is computed numerically using a Runge-Kutta method of the 4th order.

The following properties are computed:

Table 15: Conic shock properties

I	Property	Description
1	M	Mach number
2	θ	Shock angle (°)
3	σ	Cone angle (°)

3.17.2 arscow - Conical flow given M and δ

```
void arscow(double g, double m, double w, double result[3], int *ierr);
```

Solve the conical flow given a mach number M and wave angle δ .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M \geq 1$.
w	in	Wave angle $0 < \delta < 90$.
result	out	Array with result properties as described in 15.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.
- 3 Given δ out of range.
- 4 Iterative solver failed.

3.17.3 arscoms - Conical flow given M and θ

```
void arscoms(double g, double m, double s, double result[3], int *ierr);
```

Solve the conical flow given a mach number M and deflection surface angle θ .

Performance

Iterative

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M \geq 1$.
s	in	Deflection surface angle $0 < \theta < 90$.
result	out	Array with result properties as described in 15.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.
- 3 Given θ out of range.
- 4 Iterative solver failed.

3.18 Moving Normal Shock Waves

Moving normal shock waves refer to normal shock waves in linear motion axis symmetric to the flow direction. Two sets of functions are available, one computes the thermodynamic properties of moving normal shock waves as described and the other set computes the mechanical/dynamic properties of such shock waves. These are separated as the functions computing the mechanical properties will require additional arguments in comparison to the thermodynamic property functions.

3.19 Moving Normal Shock Waves (Thermodynamic Properties)

3.19.1 Introduction

This function group computes the thermodynamic properties of a moving normal shock wave.

The following properties are computed:

Table 16: Moving normal shock wave thermodynamic properties

I	Property	Description
1	M	Mach number
2	p_2/p_1	Pressure ratio
3	ρ_2/ρ_1	Density ratio
4	T_2/T_1	Temperature ratio

3.19.2 arsmnsm - Moving shock relations given M

```
void arsmnsm(double g, double m, double result[4], int *ierr);
```

Compute the moving normal shock wave relations given the mach number M .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $M > 0$.
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.19.3 arsmnsp - Moving shock relations given p_2/p_1

```
void arsmnsp(double g, double p, double result[4], int *ierr);
```

Compute the moving normal shock wave relations given the pressure ratio p_2/p_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
p	in	Pressure ratio $p_2/p_1 > (1 - \gamma)/(\gamma + 1)$.
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given p_2/p_1 out of range.

3.19.4 arsmnsd - Moving shock relations given ρ_2/ρ_1

```
void arsmnsd(double g, double d, double result[4], int *ierr);
```

Compute the moving normal shock wave relations given the density ratio ρ_2/ρ_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
d	in	Density ratio $\rho_2/\rho_1 > -(\gamma^2 - 1)/(\gamma^2 + 1)$.
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given ρ_2/ρ_1 out of range.

3.19.5 arsmnst - Moving shock relations given T_2/T_1

```
void arsmnst(double g, double t, double result[4], int *ierr);
```

Compute the moving normal shock wave relations given the temperature ratio T_2/T_1 .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
t	in	Temperature ratio $T_2/T_1 > (\gamma^2 + 1)/(\gamma + 1)^2$.
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Computed M out of range.
- 3 Given T_2/T_1 out of range.

3.20 Moving Normal Shock Waves (Dynamic Properties)

3.20.1 Introduction

This function group computes the mechanic/dynamic properties of a moving normal shock wave. These not only require the specific heat constant γ but also the speed of sound in the latter medium a_0 .

The following properties are computed:

Table 17: Moving normal shock waves dynamic properties

I	Property	Description
1	p_2/p_1	Pressure ratio
2	V	Velocity
3	U_P	Max-motion velocity, downstream

3.20.2 arsmnvp - Dynamic moving shock relations given p_2/p_1

```
void arsmnvp(double g, double a0, double p, double result[3], int *ierr);
```

Compute the dynamic moving normal shock wave relations given the the pressure ratio p_2/p_1 and the speed of sound a_0 of the medium.

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
a0	in	Speed of sound in the medium $a_0 > 0$.
p	in	Pressure ratio $p_2/p_1 > (\gamma - 1)/(\gamma + 1)$.
result	out	Array with result properties as described in 17.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given a_0 out of range.
- 3 Given p_2/p_1 out of range.

3.20.3 arsmnvw - Dynamic moving shock relations given V

```
void arsmnvw(double g, double a0, double w, double result[3], int *ierr);
```

Compute the dynamic moving normal shock wave relations given the the velocity V and the speed of sound a_0 of the medium.

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
a0	in	Speed of sound in the medium $a_0 > 0$.
w	in	Velocity $V > 0$.
result	out	Array with result properties as described in 17.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given a_0 out of range.
- 3 Computed p_2/p_1 out of range.
- 4 Given V out of range.

3.20.4 arsmnvup - Dynamic moving shock relations given U_p

```
void arsmnvup(double g, double a0, double up, double result[3], int *ierr);
```

Compute the dynamic moving normal shock wave relations given the mass-motion velocity U_p and the speed of sound a_0 of the medium.

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
a0	in	Speed of sound in the medium $a_0 > 0$.
up	in	Maxx-motion velocity $U_p > -(2\sqrt{2}a_0\sqrt{\gamma(\gamma^2 + 2\gamma - 1)})/(\gamma + 1)$.
result	out	Array with result properties as described in 17.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given a_0 out of range.
- 3 Computed p_2/p_1 out of range.
- 4 Given U_p out of range.

3.21 Karman-Tsien Pressure Correction Coefficient

3.21.1 Introduction

The *Karman-Tsien* pressure correlation coefficient is defined as:

$$C_p = \frac{C_{p0}}{\sqrt{1-M^2} + \frac{1}{2} \left(\frac{M^2}{1+\sqrt{1-M^2}} \right) C_{p0}}$$

Where C_{p0} the incompressibility coefficient.

The following properties are computed:

Table 18: Karman-Tsien property table

I	Property	Description
1	M	Mach number
2	C_p	Pressure correction coefficient
3	C_{p0}	Incompressibility coefficient

3.21.2 arckarcp - Karman-Tsien pressure correction given M and C_{p0}

```
void arckarcp(double g, double m, double cin, double result[3], int *ierr);
```

Compute the Karman-Tsien pressure correction coefficient relations given the mach number M and the the incompressibility coefficient C_{p0} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $0 < M < 0.8$.
cin	in	Incompressibility coefficient C_{p0} .
result	out	Array with result properties as described in 18.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.21.3 arckarci - Karman-Tsien pressure correction given M and C_p

```
void arckarci(double g, double m, double cp, double result[3], int *ierr);
```

Compute the Karman-Tsien pressure correction coefficient relations given the mach number M and the the Karman-Tsien pressure correction coefficient C_p .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $0 < M < 0.8$.
cp	in	Pressure correction coefficient C_p .
result	out	Array with result properties as described in 18.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.22 Laitone Pressure Correction Coefficient

3.22.1 Introduction

The *Laitone* pressure correlation coefficient is defined as:

$$C_p = \frac{C_{p0}}{\sqrt{1 - M^2} + \left(M^2 \frac{1 + (\gamma - 1)/2 \times M^2}{2\sqrt{1 - M^2}} \right) C_{p0}}$$

Where C_{p0} the incompressibility coefficient.

The following properties are computed:

Table 19: Laitone property table

I	Property	Description
1	M	Mach number
2	C_p	Pressure correction coefficient
3	C_{p0}	Incompressibility coefficient

3.22.2 arclaicp - Laitone pressure correction given M and C_{p0}

```
void arclaicp(double g, double m, double cin, double result[3], int *ierr);
```

Compute the Laitone pressure correction coefficient relations given the mach number M and the the incompressibility coefficient C_{p0} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $0 < M < 0.8$.
cin	in	Incompressibility coefficient C_{p0} .
result	out	Array with result properties as described in 19.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.22.3 arclaici - Laitone pressure correction given M and C_p

```
void arclaici(double g, double m, double cp, double result[3], int *ierr);
```

Compute the Laitone pressure correction coefficient relations given the mach number M and the the Laitone pressure correction coefficient C_p .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $0 < M < 0.8$.
cp	in	Pressure correction coefficient C_p .
result	out	Array with result properties as described in 19.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.23 Prandtl-Glauert Pressure Correction Coefficient

3.23.1 Introduction

The *Prandtl-Glauert* pressure correlation coefficient is defined as:

$$C_p = \frac{C_{p0}}{\sqrt{1-M^2}}$$

Where C_{p0} the incompressibility coefficient.

The following properties are computed:

Table 20: Prandtl-Glauert property table

I	Property	Description
1	M	Mach number
2	C_p	Pressure correction coefficient
3	C_{p0}	Incompressibility coefficient

3.23.2 arcpglcp - Prandtl-Glauert pressure correction given M and C_{p0}

```
void arcpglcp(double g, double m, double cin, double result[3], int *ierr);
```

Compute the Prandtl-Glauert pressure correction coefficient relations given the mach number M and the the incompressibility coefficient C_{p0} .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $0 < M < 0.8$.
cin	in	Incompressibility coefficient C_{p0} .
result	out	Array with result properties as described in 20.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.

3.23.3 arcpglci - Prandtl-Glauert pressure correction given M and C_p

```
void arcpglci(double g, double m, double cp, double result[3], int *ierr);
```

Compute the Prandtl-Glauert pressure correction coefficient relations given the mach number M and the the Prandtl-Glauert pressure correction coefficient C_p .

Performance

Fixed

Arguments

Argument	Intent	Description
g	in	Specific heat constant γ .
m	in	Mach number $0 < M < 0.8$.
cp	in	Pressure correction coefficient C_p .
result	out	Array with result properties as described in 20.
ierr	out	(optional) Return status code

Status codes

- 1 Specific heat ratio $\gamma \leq 1$.
- 2 Given M out of range.