

**Compressible Flow Subroutine Library  
Reference Manual (Fortran)**

**DD-00008-110**

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# Contents

<b>1</b>	<b>About this Guide</b>	<b>5</b>
1.1	Legal Information	5
1.2	Feedback and Contact	5
1.3	Introduction	5
1.4	Audience for This Guide	5
1.5	How to Use This Guide	5
1.6	Conventions Used in This Guide	5
<b>2</b>	<b>Overview</b>	<b>6</b>
2.1	Introduction	6
2.2	Performance Characteristics	6
2.3	Error Behavior	6
<b>3</b>	<b>Function Reference</b>	<b>7</b>
3.1	System functions	7
3.1.1	Introduction	7
3.1.2	arsyver - Get version information	8
3.1.3	arsyerr - Retrieve and reset error code	9
3.2	Characteristic Mach Number	10
3.2.1	Introduction	10
3.2.2	armcmm - Compute given normal mach number, $M$	11
3.2.3	armcms - Compute given characteristic mach number, $M^*$	12
3.3	Hugoniot compression	13
3.3.1	Introduction	13
3.3.2	arshud - Compute given density factor $\rho_2/\rho_1$	14
3.3.3	arshup - Compute given density factor $p_2/p_1$	15
3.4	Critical mach number	16
3.4.1	armcrm - Critical pressure coefficient given $M_{\text{crit}}$	17
3.4.2	armcrc - Critical mach number given $C_p$	18
3.4.3	armcrpg - Critical mach number given $C_{p0}$ using Prandtl-Glauert pressure approximation	19
3.4.4	armcrla - Critical mach number given $C_{p0}$ using Laitone pressure approximation	20
3.4.5	armcrkt - Critical mach number given $C_{p0}$ using Karman-Tsien pressure approximation	21
3.5	Isentropic flow	22
3.5.1	Introduction	22
3.5.2	arfism - Isentropic relations given $M$	23
3.5.3	arfisp - Isentropic relations given $p_2/p_1$	24
3.5.4	arfisd - Isentropic relations given $\rho_2/\rho_1$	25
3.5.5	arfist - Isentropic relations given $T_2/T_1$	26
3.5.6	arfisa - Isentropic relations given $A/A^*$	27
3.6	Fanno flow	28
3.6.1	Introduction	28
3.6.2	arffam - Fanno relations given $M$	29
3.6.3	arffap - Fanno relations given $p/p^*$	30
3.6.4	arffad - Fanno relations given $\rho/\rho^*$	31
3.6.5	arffat - Fanno relations given $T/T^*$	32
3.6.6	arffav - Fanno relations given $V/V^*$	33
3.6.7	arffap0 - Fanno relations given $p_{01}/p_{02}$	34
3.6.8	arffaf - Fanno relations given $(4fL)/D$	35
3.6.9	arffads - Fanno relations given $(s - s^*)/c_p$	36
3.7	Rayleigh Flow	37
3.7.1	Introduction	37
3.7.2	arfram - Rayleigh relations given $M$	38
3.7.3	arfrap - Rayleigh relations given $p/p^*$	39
3.7.4	arfrad - Rayleigh relations given $\rho/\rho^*$	40
3.7.5	arfrat - Rayleigh relations given $T/T^*$	41
3.7.6	arfrav - Rayleigh relations given $V/V^*$	42
3.7.7	arfrap0 - Rayleigh relations given $p_{02}/p_{01}$	43

3.7.8 arfrat0 - Rayleigh relations given  $T_{02}/T_{01}$  . . . . . 44

3.7.9 arfrads - Rayleigh relations given  $(s - s^*)/c_p$  . . . . . 45

3.8 Isothermal flow through long duct . . . . . 46

3.8.1 Introduction . . . . . 46

3.8.2 arfitm - Isothermal relations given  $M$  . . . . . 47

3.8.3 arfitv - Isothermal relations given  $V/V^*$  . . . . . 48

3.8.4 arfits - Isothermal relations given  $p^*/p, r^*/r, M^*/M$  . . . . . 49

3.8.5 arfitp0 - Isothermal relations given  $p_{01}/p_{02}$  . . . . . 50

3.8.6 arfitt0 - Isothermal relations given  $T_{02}/T_{01}$  . . . . . 51

3.8.7 arfitf - Isothermal relations given  $(4fL)/D$  . . . . . 52

3.9 DeLaval nozzle flow . . . . . 53

3.9.1 Introduction . . . . . 53

3.9.2 arfqism - DeLaval isentropic flow relations given  $M$  . . . . . 54

3.9.3 arfqisp - DeLaval isentropic flow relations given  $p/p_1$  . . . . . 55

3.9.4 arfqisd - DeLaval isentropic flow relations given  $\rho/\rho_1$  . . . . . 56

3.9.5 arfqist - DeLaval isentropic flow relations given  $T/T_1$  . . . . . 57

3.9.6 arfqisa - DeLaval isentropic flow relations given  $A/A^*$  . . . . . 58

3.10 Normal Shock Waves . . . . . 59

3.10.1 Introduction . . . . . 59

3.10.2 arsnsm1 - Normal shock relations given  $M_{1n}$  . . . . . 60

3.10.3 arsnsm2 - Normal shock relations given  $M_{2n}$  . . . . . 61

3.10.4 arsnsp - Normal shock relations given  $p_2/p_1$  . . . . . 62

3.10.5 arnsnd - Normal shock relations given  $\rho_2/\rho_1$  . . . . . 63

3.10.6 arsnst - Normal shock relations given  $T_2/T_1$  . . . . . 64

3.10.7 arsnsp0 - Normal shock relations given  $p_{02}/p_{01}$  . . . . . 65

3.11 Oblique Shock Relations . . . . . 66

3.11.1 Introduction . . . . . 66

3.11.2 arsolmw - Oblique shock relations given  $M_1$  and  $\delta$  . . . . . 67

3.11.3 arsolpw - Oblique shock relations given  $p_2/p_1$  and  $\delta$  . . . . . 68

3.11.4 arsoldw - Oblique shock relations given  $\rho_2/\rho_1$  and  $\delta$  . . . . . 69

3.11.5 arsoltw - Oblique shock relations given  $T_2/T_1$  and  $\delta$  . . . . . 70

3.11.6 arsolp0w - Oblique shock relations given  $p_{02}/p_{01}$  and  $\delta$  . . . . . 71

3.11.7 arsolws - Oblique shock relations given  $\theta$  and  $\delta$  . . . . . 72

3.11.8 arsolms - Oblique shock relations given  $M_1$  and  $\theta$  . . . . . 73

3.12 Oblique Shock Limits . . . . . 74

3.12.1 Introduction . . . . . 74

3.12.2 arsolld - Compute maximum wave and deflection surface angle before shock detachment . . . . . 75

3.12.3 arsollls - Compute maximum wave and deflection surface angle that wil result in sonic down-stream flow . . . . . 76

3.13 Prandtl-Meyer function . . . . . 77

3.13.1 Introduction . . . . . 77

3.13.2 arspmm - Prandtl-Meyer properties given  $M$  . . . . . 78

3.13.3 arspmv - Prandtl-Meyer properties given  $v(M)$  . . . . . 79

3.13.4 arspmt - Prandtl-Meyer properties given  $\theta$  . . . . . 80

3.13.5 arspmfm - Prandtl-Meyer angle from  $M$  . . . . . 81

3.13.6 arspmfv - Mach number from  $v(M)$  . . . . . 82

3.14 Expansion Fan (Rarefaction Wave) . . . . . 83

3.14.1 Introduction . . . . . 83

3.14.2 arsefm - Expansion fan properties given  $M_1$  and  $M_2$  . . . . . 84

3.14.3 arsefp - Expansion fan properties given  $p_2/p_1$  and either  $M_1$  or  $M_2$  . . . . . 85

3.14.4 arsefd - Expansion fan properties given  $\rho_2/\rho_1$  and either  $M_1$  or  $M_2$  . . . . . 86

3.14.5 arseft - Expansion fan properties given  $T_2/T_1$  and either  $M_1$  or  $M_2$  . . . . . 87

3.15 (Rayleigh-)Pitot Tube Relations . . . . . 88

3.15.1 Introduction . . . . . 88

3.15.2 arspmt - (Rayleigh-)Pitot relations given  $M$  . . . . . 89

3.15.3 arsppt - (Rayleigh-)Pitot relations given  $p_0/p$  or  $p_{02}/p_1$  . . . . . 90

3.16 Reflected Shock Waves . . . . . 91

3.16.1 Introduction . . . . . 91

3.16.2 arsrms - Reflected shock wave mach number given  $M$  . . . . . 92

3.16.3 arsrsmr - Incident shock wave mach number given  $M'$  . . . . . 93

3.17 Quasi-2D Conical Flow . . . . . 94

3.17.1 Introduction . . . . . 94

3.17.2 arskomw - Conical flow given  $M$  and  $\delta$  . . . . . 95

3.17.3 arskomc - Conical flow given  $M$  and  $\theta$  . . . . . 96

3.18 Moving Normal Shock Waves . . . . . 97

3.19 Moving Normal Shock Waves (Thermodynamic Properties) . . . . . 97

3.19.1 Introduction . . . . . 97

3.19.2 arsmnsm - Moving shock relations given  $M$  . . . . . 98

3.19.3 arsmnsp - Moving shock relations given  $p_2/p_1$  . . . . . 99

3.19.4 arsmnsd - Moving shock relations given  $\rho_2/\rho_1$  . . . . . 100

3.19.5 arsmnst - Moving shock relations given  $T_2/T_1$  . . . . . 101

3.20 Moving Normal Shock Waves (Dynamic Properties) . . . . . 102

3.20.1 Introduction . . . . . 102

3.20.2 arsmnvp - Dynamic moving shock relations given  $p_2/p_1$  . . . . . 103

3.20.3 arsmnvw - Dynamic moving shock relations given  $V$  . . . . . 104

3.20.4 arsmnvup - Dynamic moving shock relations given  $U_p$  . . . . . 105

3.21 Karman-Tsien Pressure Correction Coefficient . . . . . 106

3.21.1 Introduction . . . . . 106

3.21.2 arckarcp - Karman-Tsien pressure correction given  $M$  and  $C_{p0}$  . . . . . 107

3.21.3 arckarci - Karman-Tsien pressure correction given  $M$  and  $C_p$  . . . . . 108

3.22 Laitone Pressure Correction Coefficient . . . . . 109

3.22.1 Introduction . . . . . 109

3.22.2 arclai cp - Laitone pressure correction given  $M$  and  $C_{p0}$  . . . . . 110

3.22.3 arclai ci - Laitone pressure correction given  $M$  and  $C_p$  . . . . . 111

3.23 Prandtl-Glauert Pressure Correction Coefficient . . . . . 112

3.23.1 Introduction . . . . . 112

3.23.2 arcp gl cp - Prandtl-Glauert pressure correction given  $M$  and  $C_{p0}$  . . . . . 113

3.23.3 arcp gl ci - Prandtl-Glauert pressure correction given  $M$  and  $C_p$  . . . . . 114

# 1 About this Guide

## 1.1 Legal Information

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## 1.3 Introduction

This manual describes the *Application Programming Interface* (API) of the *Compressible Flow Subroutine Library* for the Fortran programming language families.

## 1.4 Audience for This Guide

The audience of this guide is assumed to be Fortran programmers who understand the basic concepts of at least one of the aforementioned programming languages.

## 1.5 How to Use This Guide

This guide first describes some general programming details of the library and then documents each function individually.

## 1.6 Conventions Used in This Guide

*x*

Normal math typesetting represents a normal variable.

**x**

Bold math typesetting represents a vector.

Mono

Monospace typesetting represents C function names, variables or data types.

## 2 Overview

### 2.1 Introduction

### 2.2 Performance Characteristics

Each function or subroutine has a declared performance characteristic, these represent how the performance of a function can be predicted.

**Fixed** The function always executes around the same amount of instructions. Depending upon the actual values passed in the arguments there might be insignificant variations but do not contain any iterative solver. The behavior of standard library functions used is not considered for this performance classification.

**Iterative** The function uses an iterative root finding algorithm to compute the result. In the library all functions which use iterative solvers have a maximum amount of iterations, after which they will fail.

Iterative solvers are usually non-linear root finding methods such as Newton-Raphson, False Position or Bisection style solvers or can be solvers for differential equations such as Runge-Kutta methods as described in [DKahaner1988].

### 2.3 Error Behavior

All library subroutines where an error may occur usually have an optional integer pointer argument. If the latter is given and an error occurs the error code will be written into the integer at the pointer's location. If no error occurs the integer will not be changed. As such this allows by design a logical-OR behavior in which one may call several subroutines and check at the very end whether an error code has been set.

This error code is also set into a *thread-local* variable and can be inquired using the 3.1.3 function for the current thread. The latter will also provide the name of the offending function for easier traceback.

Functions that are designed for specific purposes may however return NaN (*Not-a-Number*) or infinity  $\infty$ . The specific error behavior for those is documented for each of such functions individually.

## **3 Function Reference**

### **3.1 System functions**

#### **3.1.1 Introduction**

The functions in this group provide system information about the CFSL library and error handling facilities.

**3.1.2 arsyver - Get version information**

```
SUBROUTINE ARO1AA(MAJOR, MINOR, CMPLR)
  INTEGER MAJOR, MINOR
  CHARACTER CMPLR(16)
```

Return the major, minor version and the compiler used to compile the library.

**Arguments**

<b>Argument</b>	<b>Intent</b>	<b>Description</b>
major	out	<i>(optional)</i> Pointer to store major version in
minor	out	<i>(optional)</i> Pointer to store minor version in
cmplr	out	<i>(optional)</i> Pointer to store a pointer to the compiler version string

**3.1.3 arsyerr - Retrieve and reset error code**

INTEGER FUNCTION AR01AB(FN, CLEAR)

CHARACTER FN(16)

LOGICAL CLEAR

Returns the last error code and messages that occurred in the current thread.

**Parameters**

Argument	Intent	Description
fn	out	( <i>optional</i> ) Pointer to store a pointer to the function name string
clear	in	Whether to clear the error code from the <i>thread-local</i> context

## 3.2 Characteristic Mach Number

### 3.2.1 Introduction

This function group computes the characteristic Mach Number  $M^*$  as given in [JDAnderson1982] and [Shapiro1953] from a given mach number  $M$  or in reverse the latter given  $M^*$ . The characteristic mach number has the following properties:

$$\begin{aligned} M^* &= 0 && \text{if } M = 0 \\ M^* &= 1 && \text{if } M = 1 \\ M^* &< 1 && \text{if } M < 1 \\ M^* &> 1 && \text{if } M > 1 \end{aligned}$$

And furthermore the its most useful property:

$$\lim_{M \rightarrow \infty} M^* = \sqrt{\frac{\gamma + 1}{\gamma - 1}}$$

The following properties are computed:

Table 1: Characteristic mach number properties

<b>I</b>	<b>Symbol</b>	<b>Description</b>
1	$M$	Mach number
2	$M^*$	Characteristic mach number

**3.2.2 armcmm - Compute given normal mach number,  $M$** 

```
DOUBLE PRECISION FUNCTION ARO2AA(G,M,IERR)
  DOUBLE PRECISION G, M
  INTEGER IERR
```

Compute given normal mach number,  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$
m	in	Mach number $M > 0$
ierr	out	(optional) Return status code

**Status Codes**

-1 Specific heat ratio  $\gamma \leq 1$ .

-2 Given  $M \leq 0$ .

**Return Value**

Characteristic mach number  $M^*$  or NAN on error.

**3.2.3 armcms - Compute given characteristic mach number,  $M^*$** 

```
DOUBLE PRECISION FUNCTION ARO2AB(G,MSTAR,IERR)
  DOUBLE PRECISION G, MSTAR
  INTEGER IERR
```

Compute given the characteristic mach number,  $M^*$ . Note that if  $M^* = \sqrt{(\gamma+1)(\gamma-1)}$  the function will return  $M = \infty = \text{INFINITY}$ .

**Performance**

Fixed

**Parameters**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$
mstar	in	Characteristic mach number $0 < M^* \leq \sqrt{(\gamma+1)(\gamma-1)}$ .
ierr	out	(optional) Return status code

**Status Codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 3 Given  $M^*$  out of specified range.

**Return Value**

Normal mach number  $M$  or NAN on error.

### 3.3 Hugoniot compression

#### 3.3.1 Introduction

Hugoniot's equation can be used to model a normal shock wave by thermodynamic constants only as given by [JAnderson1982]. As such this equation allows the relation of the pressure factor over the shock wave  $p_2/p_1$  to the density factor over the same  $\rho_2/\rho_1$  given a specific heat constant  $\gamma$  without being related to a velocity or mach number. Note that the Hugoniot based shock wave compression does not yield exactly the same results as normal shock wave relations and in fact deviates from them at higher mach numbers. The following properties are computed:

Table 2: Hugoniot compression properties

<b>I</b>	<b>Symbol</b>	<b>Description</b>
1	$p_2/p_1$	Pressure factor
2	$\rho_2/\rho_1$	Density factor

**3.3.2 arshud - Compute given density factor  $\rho_2/\rho_1$** 

```
DOUBLE PRECISION FUNCTION ARO3AA(G,D,IERR)
  DOUBLE PRECISION G, D
  INTEGER IERR
```

Compute pressure factor based upon density factor  $\rho_2/\rho_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density fraction $0 < \rho_2/\rho_1 < \sqrt{\frac{\gamma+1}{\gamma-2}}$ .
ierr	out	( <i>optional</i> ) Return status code.

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $\rho_2/\rho_1$  out of range.

**Return Value**

Pressure fraction  $p_2/p_1$  or NAN on error.

**3.3.3 arshup - Compute given density factor  $p_2/p_1$** 

```
DOUBLE PRECISION FUNCTION ARO3AB(G,P,IERR)
  DOUBLE PRECISION G, P
  INTEGER IERR
```

Compute pressure factor based upon pressure factor  $p_2/p_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure fraction $p_2/p_1 > 0$ .
ierr	out	(optional) Return status code.

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $p_2/p_1$  out of range.

**Return Value**

Density fraction  $\rho_2/\rho_1$  or NAN on error.

### **3.4 Critical mach number**

**3.4.1 armcrm - Critical pressure coefficient given  $M_{\text{crit}}$** 

```
DOUBLE PRECISION FUNCTION ARO4AA(G,MCRIT,IERR)
  DOUBLE PRECISION G, MCRIT
  INTEGER IERR
```

Compute given the critical pressure coefficient given  $M_{\text{crit}}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
mcrit	in	Critical Mach number $0 < M_{\text{crit}} < 1$ .
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_{\text{crit}}$  out of range.

**Return Value**

Critical pressure coefficient  $C_p$  or NAN on error.

**3.4.2 armcrc - Critical mach number given  $C_p$** 

DOUBLE PRECISION FUNCTION ARO4AB(G,CP,IERR)  
 DOUBLE PRECISION G, CP  
 INTEGER IERR

Compute given the critical mach number given  $C_p$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
cp	in	Critical pressure coefficient $C_p$ .
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $C_p$  out of range.
- 3 Iterative solver failed.

**Return Value**

Critical mach number  $M_{crit}$  or NAN on error.

**3.4.3 armcrpg - Critical mach number given  $C_{p0}$  using Prandtl-Glauert pressure approximation**

```
DOUBLE PRECISION FUNCTION ARO4AC(G,CPO,IERR)
  DOUBLE PRECISION G, CPO
  INTEGER IERR
```

Compute critical mach number given  $C_{p0}$  Prandtl-Glauert pressure approximation.

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
cp0	in	Critical pressure coefficient $C_{p0}$ .
ierr	out	(optional) Return status code

**Status codes**

-1 Specific heat ratio  $\gamma \leq 1$ .

-2 Iterative solver failed.

**Return Value**

Critical mach number  $M_{crit}$  or NAN on error.

**3.4.4 armcrla - Critical mach number given  $C_{p0}$  using Laitone pressure approximation**

```
DOUBLE PRECISION FUNCTION ARO4AD(G,CPO,IERR)
  DOUBLE PRECISION G, CPO
  INTEGER IERR
```

Compute critical mach number given  $C_{p0}$  Laitone pressure approximation.

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
cp0	in	Critical pressure coefficient $C_{p0}$ .
ierr	out	(optional) Return status code

**Status codes**

-1 Specific heat ratio  $\gamma \leq 1$ .

-2 Iterative solver failed.

**Return Value**

Critical mach number  $M_{crit}$  or NAN on error.

**3.4.5 armcrkt - Critical mach number given  $C_{p0}$  using Karman-Tsien pressure approximation**

```
DOUBLE PRECISION FUNCTION ARO4AE(G,CPO,IERR)
  DOUBLE PRECISION G, CPO
  INTEGER IERR
```

Compute critical mach number given  $C_{p0}$  Karman-Tsien pressure approximation.

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
cp0	in	Critical pressure coefficient $C_{p0}$ .
ierr	out	(optional) Return status code

**Status codes**

-1 Specific heat ratio  $\gamma \leq 1$ .

-2 Iterative solver failed.

**Return Value**

Critical mach number  $M_{crit}$  or NAN on error.

## 3.5 Isentropic flow

### 3.5.1 Introduction

This function group computes the thermodynamic properties of isentropic flow for a calorically perfect gas as described in [naca1135] with one-dimensional variable changes. Isentropic flow assumes the following continuity equation:

$$\rho AV = \text{const}$$

The momentum equation is:

$$p + \rho AV^2 = \text{const}$$

The following properties are computed:

Table 3: Isentropic flow properties

I	Property	Description
1	$M$	Mach number
2	$p_0/p_1$	Pressure ratio
3	$\rho_0/\rho_1$	Density ratio
4	$T_0/T_1$	Temperature ratio
5	$A/A^*$	Critical area ratio

**3.5.2 arfism - Isentropic relations given  $M$** 

```

SUBROUTINE ARO5AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(5)
  INTEGER IERR

```

Compute the isentropic relations given the mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 3.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.5.3 arfisp - Isentropic relations given  $p_2/p_1$** 

```

SUBROUTINE ARO5AB(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(5)
  INTEGER IERR

```

Compute the isentropic relations given the pressure ratio  $p_2/p_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $0 \leq p_2/p_1 \leq 1$ .
result	out	Array with result properties as described in 3.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p_2/p_1$  out of range.

**3.5.4 arfisd - Isentropic relations given  $\rho_2/\rho_1$** 

```

SUBROUTINE ARO5AC(G,D,RESULT,IERR)
  DOUBLE PRECISION G, D, RESULT(5)
  INTEGER IERR

```

Compute the isentropic relations given the density ratio  $\rho_2/\rho_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
r	in	Density ratio $0 \leq \rho_2/\rho_1 \leq 1$ .
result	out	Array with result properties as described in 3.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $\rho_2/\rho_1$  out of range.

**3.5.5 arfist - Isentropic relations given  $T_2/T_1$** 

```

SUBROUTINE ARO5AD(G,T,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(5)
  INTEGER IERR

```

Compute the isentropic relations given the temperature ratio  $T_2/T_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $0 \leq T_2/T_1 \leq 1$ .
result	out	Array with result properties as described in 3.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $T_2/T_1$  out of range.

**3.5.6 arfisa - Isentropic relations given  $A/A^*$** 

```

SUBROUTINE ARO5AE(G,A,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, A, RESULT(5)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the isentropic relations given the critical area ratio  $A/A^*$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
a	in	Critical area ratio $A/A^* \geq 1$ .
is_sub	in	Whether the mach number corresponding to $A/A^*$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 3.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $A/A^*$  out of range.
- 4 Iterative solver failed

## 3.6 Fanno flow

### 3.6.1 Introduction

This function group computes the thermodynamic properties of adiabatic flow with friction for calorically perfect gas as described in [JAnderson1982].

The following properties are computed:

Table 4: Fanno flow properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$p/p^*$	Pressure ratio
3	$\rho/\rho^*$	Density ratio
4	$T/T^*$	Temperature ratio
5	$V/V^*$	Velocity ratio
6	$p_{01}/p_{02}$	Stagnation pressure ratio
7	$(4fL)/D$	Fanno line
8	$(s - s^*)/c_p$	Change in entropy

**3.6.2 arffam - Fanno relations given  $M$** 

```

SUBROUTINE ARO6AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(8)
  INTEGER IERR

```

**Description**

Compute the fanno relations given a mach number,  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 4.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.6.3 arffap - Fanno relations given  $p/p^*$** 

```

SUBROUTINE AROGAB(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(8)
  INTEGER IERR

```

Compute the fanno relations given the pressure ratio,  $p/p^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $0 \leq p/p^*$ .
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p/p^*$  out of range.

**3.6.4 arffad - Fanno relations given  $\rho/\rho^*$** 

```

SUBROUTINE ARO6AC(G,D,RESULT,IERR)
  DOUBLE PRECISION G, D, RESULT(8)
  INTEGER IERR

```

Compute the fanno relations given the density ratio,  $\rho/\rho^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $\sqrt{(\gamma-1)/(\gamma+1)} \leq \rho/\rho^*$ .
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $\rho/\rho^*$  out of range.

**3.6.5 arffat - Fanno relations given  $T/T^*$** 

```

SUBROUTINE ARO6AD(G,T,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(8)
  INTEGER IERR

```

Compute the fanno relations given the temperature ratio,  $T/T^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $0 \leq T/T^* \leq (\gamma + 1)/(\gamma - 1)$ .
result	out	Array with result properties as described in 4.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $T/T^*$  out of range.

**3.6.6 arffav - Fanno relations given  $V/V^*$** 

```

SUBROUTINE ARO6AE(G,V,RESULT,IERR)
  DOUBLE PRECISION G, V, RESULT(8)
  INTEGER IERR

```

Compute the fanno relations given the velocity ratio,  $V/V^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
v	in	Velocity ratio $0 \leq V/V^* \leq \sqrt{(\gamma+1)/(\gamma-1)}$ .
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $V/V^*$  out of range.

**3.6.7 arffap0 - Fanno relations given  $p_{01}/p_{02}$** 

```

SUBROUTINE ARO6AF(G,PO,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, PO, RESULT(8)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the fanno relations given the stagnation pressure ratio,  $p_{01}/p_{02}$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p0	in	Stagnation pressure ratio $1 \leq p_{02}/p_{01}$ .
is_sub	in	Whether $M$ corresponding to the given $p_{02}/p_{01}$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p_{01}/p_{02}$  out of range.
- 4 Iterative solver failed.

**3.6.8 arffaf - Fanno relations given  $(4fL)/D$** 

```

SUBROUTINE ARO6AG(G,L,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, L, RESULT(8)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the fanno relations given the fanno line,  $(4fL)/D$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
l	in	Fanno line $0 \leq (4fL)/D \leq ((\gamma + 1)\log((\gamma + 1)/(\gamma - 1)) - 2)/(2\gamma)$ .
is_sub	in	Whether $M$ corresponding to the given $(4fL)/D$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $(4fL)/D$  out of range.
- 4 Iterative solver failed.

**3.6.9 arffads - Fanno relations given  $(s - s^*)/c_p$** 

```

SUBROUTINE ARO6AH(G,DS,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, DS, RESULT(8)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the fanno relations given the fanno line,  $(s - s^*)/c_p$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
ds	in	Change in entropy $-\infty < (s - s^*)/c_p < \infty$ .
is_sub	in	Whether $M$ corresponding to the given $(s - s^*)/c_p$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 4.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $(s - s^*)/c_p$  out of range.
- 4 Iterative solver failed.

## 3.7 Rayleigh Flow

### 3.7.1 Introduction

This function group computes the thermodynamic properties of non-adiabatic flow with heat addition for a calorically perfect gas as described in [JDAnderson1982].

The computed properties are as follows:

Table 5: Rayleigh flow properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$p/p^*$	Pressure ratio
3	$\rho/\rho^*$	Density ratio
4	$T/T^*$	Temperature ratio
5	$V/V^*$	Velocity ratio
6	$p_{01}/p_{02}$	Stagnation pressure ratio
7	$T_{01}/T_{02}$	Stagnation temperature ratio
8	$(s - s^*)/c_p$	Change in entropy

**3.7.2 arfram - Rayleigh relations given  $M$** 

```

SUBROUTINE ARO7AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(8)
  INTEGER IERR

```

Compute the rayleigh relations given a mach number,  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 5.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.7.3 arfrac - Rayleigh relations given  $p/p^*$** 

```

SUBROUTINE ARO7AB(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(8)
  INTEGER IERR

```

Compute the rayleigh relations given the pressure ratio,  $p/p^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $0 < p/p^* < \gamma + 1$ .
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p/p^*$  out of range.

**3.7.4 arfrad - Rayleigh relations given  $\rho/\rho^*$** 

```

SUBROUTINE ARO7AC(G,D,RESULT,IERR)
  DOUBLE PRECISION G, D, RESULT(8)
  INTEGER IERR

```

Compute the rayleigh relations given the density ratio,  $\rho/\rho^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $\gamma(\gamma + 1) < \rho/\rho^*$ .
result	out	Array with result properties as described in 5.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $\rho/\rho^*$  out of range.

**3.7.5 arfrac - Rayleigh relations given  $T/T^*$** 

```

SUBROUTINE ARO7AD(G,T,TMAX,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(8)
  LOGICAL TMAX
  INTEGER IERR

```

Compute the rayleigh relations given the temperature ratio,  $T/T^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $0 < T/T^*$ .
tmax	in	Whether the static temperature ratio supplied is for a low speed false or a high speed true.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $T/T^*$  out of range.

**3.7.6 arfrac - Rayleigh relations given  $V/V^*$** 

```

SUBROUTINE ARO7AE(G,V,RESULT,IERR)
  DOUBLE PRECISION G, V, RESULT(8)
  INTEGER IERR

```

Compute the rayleigh relations given the velocity ratio,  $V/V^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
v	in	Velocity ratio $0 < V/V^* < (\gamma + 1)/\gamma$ .
result	out	Array with result properties as described in 5.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $V/V^*$  out of range.

**3.7.7 arfrap0 - Rayleigh relations given  $p_{02}/p_{01}$** 

```

SUBROUTINE ARO7AF(G,PO,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, PO, RESULT(8)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the rayleigh relations given the stagnation pressure ratio,  $p_{02}/p_{01}$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p0	in	Stagnation pressure ratio $p_{02}/p_{01} > \frac{\gamma^2-1}{\gamma^2}$ .
is_sub	in	Whether $M$ corresponding to the given $p_{02}/p_{01}$ is assumed to be sub- or super-sonic.
result	out	Array with result properties as described in 5.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p_{02}/p_{01}$  out of range.
- 4 Iterative solver failed.

**3.7.8 arfrac0 - Rayleigh relations given  $T_{02}/T_{01}$** 

```

SUBROUTINE ARO7AG(G,TO,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, TO, RESULT(8)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the rayleigh relations given the stagnation temperature ratio,  $T_{02}/T_{01}$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t0	in	Stagnation temperature ratio $T_{02}/T_{01} \geq 0$ .
is_sub	in	Whether $M$ corresponding to the given $T_{02}/T_{01}$ is assumed to be sub- or super-sonic.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $T_{02}/T_{01}$  out of range.
- 4 Iterative solver failed.

**3.7.9 arfrads - Rayleigh relations given  $(s - s^*)/c_p$** 

```

SUBROUTINE ARO7AH(G,DS,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, DS, RESULT(8)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the rayleigh relations given the fanno line,  $(s - s^*)/c_p$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
ds	in	Change in entropy $-\infty < (s - s^*)/c_p < \infty$ .
is_sub	in	Whether $M$ corresponding to the given $(s - s^*)/c_p$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 5.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $(s - s^*)/c_p$  out of range.
- 4 Iterative solver failed.

## 3.8 Isothermal flow through long duct

### 3.8.1 Introduction

This function group computes an isothermal flow through a long ducts as described in [VLStreeter1966] for which neither fanno nor rayleigh flow is applicable due to the assumptions of the two latter.

The following properties are computed:

Table 6: Isothermal flow properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$\frac{p^*}{p}, \frac{r^*}{r}, \frac{M^*}{M}$	Non-stagnative ratios
3	$\rho/\rho^*$	Density ratio
5	$V/V^*$	Velocity ratio
6	$p_{01}/p_{02}$	Stagnation pressure ratio
6	$T_{01}/T_{02}$	Stagnation temperature ratio
7	$(4fL)/D$	Characteristic line

**3.8.2 arfitm - Isothermal relations given  $M$** 

```

SUBROUTINE AROSAA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(6)
  INTEGER IERR

```

Compute the isothermal relations given the mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 6.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.8.3 arfitv - Isothermal relations given  $V/V^*$** 

```

SUBROUTINE AROSAB(G,V,RESULT,IERR)
  DOUBLE PRECISION G, V, RESULT(6)
  INTEGER IERR

```

Compute the isothermal relations given the velocity ratio,  $V/V^*$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
v	in	Velocity ratio $V/V^* > 0$ .
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $V/V^*$  out of range.

**3.8.4 arfits - Isothermal relations given  $p^*/p, r^*/r, M^*/M$** 

```

SUBROUTINE AROSAC(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(6)
  INTEGER IERR

```

Compute the isothermal relations given a non-stagnative ratio,  $p^*/p, r^*/r, M^*/M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
s	in	Non-stagnative ratio $p^*/p, r^*/r, M^*/M > 0$ .
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given non-stagnative ratio out of range.

**3.8.5 arfitp0 - Isothermal relations given  $p_{01}/p_{02}$** 

```

SUBROUTINE ARO8AD(G,PO,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, PO, RESULT(6)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the isothermal relations given the stagnation pressure ratio,  $p_{01}/p_{02}$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p0	in	Stagnation pressure ratio $1 \leq p_{02}/p_{01}$ .
is_sub	in	Whether $M$ corresponding to the given $p_{02}/p_{01}$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p_{01}/p_{02}$  out of range.
- 4 Iterative solver failed.

**3.8.6 arfitt0 - Isothermal relations given  $T_{02}/T_{01}$** 

```

SUBROUTINE ARO8AE(G,TO,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, TO, RESULT(6)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the isothermal relations given the stagnation temperature  $T_{02}/T_{01}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t0	in	Stagnation temperature $T_{02}/T_{01} > 0$ .
result	out	Array with result properties as described in 6.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $T_{02}/T_{01}$  out of range.

**3.8.7 arfitf - Isothermal relations given  $(4fL)/D$** 

```

SUBROUTINE ARO8AF(G,F,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, F, RESULT(6)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the isothermal relations given the characteristic line,  $(4fL)/D$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
l	in	Characteristic line $(4fL)/D$ .
is_sub	in	Whether $M$ corresponding to the given $(4fL)/D$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 6.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $(4fL)/D$  out of range.
- 4 Iterative solver failed.

## 3.9 DeLaval nozzle flow

### 3.9.1 Introduction

This function group computes the properties of *quasi-2D* isentropic flow through a DeLaval nozzle, as described in [JDAnderson1982].

The following properties are computed:

Table 7: DeLaval nozzle properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$p/p_1$	Pressure ratio
3	$\rho/\rho^*$	Density ratio
4	$T/T_1$	Temperature ratio
5	$A/A_1$	Critical area ratio

**3.9.2 arfqism - DeLaval isentropic flow relations given  $M$** 

```

SUBROUTINE ARO9AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(5)
  INTEGER IERR

```

Compute the DeLaval nozzle isentropic relations given the mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 7.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.9.3 arfqisp - DeLaval isentropic flow relations given  $p/p_1$** 

```

SUBROUTINE ARO9AB(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(5)
  INTEGER IERR

```

Compute the DeLaval nozzle isentropic relations given the pressure ratio  $p/p_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $0 < p/p_1 < 1$ .
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p/p_1$  out of range.

**3.9.4 arfqisd - DeLaval isentropic flow relations given  $\rho/\rho_1$** 

```

SUBROUTINE ARO9AC(G,D,RESULT,IERR)
  DOUBLE PRECISION G, D, RESULT(5)
  INTEGER IERR

```

Compute the DeLaval nozzle isentropic relations given the density ratio  $p/p_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $0 < \rho/\rho_1 < 1$ .
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $\rho/\rho_1$  out of range.

**3.9.5 arfqist - DeLaval isentropic flow relations given  $T/T_1$** 

```

SUBROUTINE ARO9AD(G,T,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(5)
  INTEGER IERR

```

Compute the DeLaval nozzle isentropic relations given the temperature ratio  $T/T_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $0 < T/T_1 < 1$ .
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $T/T_1$  out of range.

**3.9.6 arfqisa - DeLaval isentropic flow relations given  $A/A^*$** 

```

SUBROUTINE ARO9AE(G,A,IS_SUB,RESULT,IERR)
  DOUBLE PRECISION G, A, RESULT(5)
  LOGICAL IS_SUB
  INTEGER IERR

```

Compute the DeLaval nozzle isentropic relations given the critical area ratio  $A/A^*$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
a	in	Critical area ratio $A/A^* > 1$ .
is_sub	in	Whether the mach number corresponding to $A/A^*$ is assumed to be sub- or super- sonic.
result	out	Array with result properties as described in 7.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $A/A^*$  out of range.
- 4 Iterative solver failed.

## 3.10 Normal Shock Waves

### 3.10.1 Introduction

These functions compute the thermodynamic properties across a normal shock wave, assuming a calorically perfect gas and an adiabatic and frictionless flow, as described in [naca1135]. It can compute the following set of properties given one of the properties in conjunction with a specific heat ratio  $\gamma$  of the gas medium.

The following equations govern normal shock waves as implemented in the function group:

Equation of Mass

$$p_1 u_1 = p_2 u_2$$

Equation of Momentum

$$p_1 + \rho_1 u_1^2 = p_2 + \rho_2 u_2^2$$

Equation of Energy

$$\frac{1}{2} u_1^2 + h_1 = \frac{1}{2} u_2^2 + h_2 \text{ [adiab]}$$

Normal Shock Waves are classified by the following properties, where the subscript 1,2 refers to upstream and downstream, respectively.

The following properties are computed:

Table 8: Normal shock properties

I	Property	Description
1	$M_{1n}$	Upstream mach number
2	$M_{2n}$	Downstream mach number
3	$p_2/p_1$	Pressure ratio
4	$\rho_2/\rho_1$	Density ratio
5	$T_2/T_1$	Temperature ratio
6	$p_{02}/p_{01}$	Stagnation pressure ratio

**3.10.2 arsnsm1 - Normal shock relations given  $M_{1n}$** 

```

SUBROUTINE AR10AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(5)
  INTEGER IERR

```

Compute the normal shock relations given the upstream mach number  $M_{1n}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Upstream number $M_{1n} \geq 1$ .
result	out	Array with result properties as described in 8.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_{1n}$  out of range.

**3.10.3 arsnsm2 - Normal shock relations given  $M_{2n}$** 

```

SUBROUTINE AR10AB(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(5)
  INTEGER IERR

```

Compute the normal shock relations given the downstream mach number  $M_{2n}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Upstream number $M_{2n} > 0$ .
result	out	Array with result properties as described in 8.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_{2n}$  out of range.

**3.10.4 arsnsp - Normal shock relations given  $p_2/p_1$** 

```

SUBROUTINE AR10AC(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(5)
  INTEGER IERR

```

Compute the normal shock relations given the pressure ratio  $p_2/p_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $p_2/p_1 < 1$ .
result	out	Array with result properties as described in 8.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M_{1n}$  out of range.
- 3 Given  $p_2/p_1$  out of range.

**3.10.5 arsnsd - Normal shock relations given  $\rho_2/\rho_1$** 

```

SUBROUTINE AR10AD(G,D,RESULT,IERR)
  DOUBLE PRECISION G, D, RESULT(5)
  INTEGER IERR

```

Compute the normal shock relations given the density ratio  $\rho_2/\rho_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $1 \leq \rho_2/\rho_1 \leq (\gamma + 1)/(\gamma - 1)$ .
result	out	Array with result properties as described in 8.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M_{1n}$  out of range.
- 3 Given  $\rho_2/\rho_1$  out of range.

**3.10.6 arsnst - Normal shock relations given  $T_2/T_1$** 

```

SUBROUTINE AR10AE(G,T,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(5)
  INTEGER IERR

```

Compute the normal shock relations given the temperature ratio  $T_2/T_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $T_2/T_1 \geq 1$ .
result	out	Array with result properties as described in 8.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M_{1n}$  out of range.
- 3 Given  $T_2/T_1$  out of range.

**3.10.7** arsnsp0 - Normal shock relations given  $p_{02}/p_{01}$ 

```

SUBROUTINE AR10AF(G,PO,RESULT,IERR)
  DOUBLE PRECISION G, PO, RESULT(5)
  INTEGER IERR

```

Compute the normal shock relations given the stagnation pressure ratio  $p_{02}/p_{01}$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p0	in	Stagnation pressure ratio $0 \leq p_{02}/p_{01} \leq 1$ .
result	out	Array with result properties as described in 8.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M_{1n}$  out of range.
- 3 Given  $p_{02}/p_{01}$  out of range.
- 4 Iterative solver failed.

## 3.11 Oblique Shock Relations

### 3.11.1 Introduction

This function group computes the thermodynamic properties of an oblique shock wave given either a mach number and the surface deflection or wave angle or based upon both the wave and deflection surface angles, using algorithms as described in [usafv1], [naca1135] and [NASA187173].

Oblique Shock Waves are classified by the following properties, where the subscript 1,2 refers to upstream and downstream, respectively. The normal mach numbers  $M_{1n}$  and  $M_{2n}$  represent the mach numbers through the shock front as by the normal shock wave equations.

The following properties will be available:

Table 9: Oblique shock properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M_1$	Upstream mach number
2	$M_2$	Downstream mach number
3	$M_{1n}$	Normal upstream mach number
4	$M_{2n}$	Normal downstream mach number
5	$\theta$	Deflection surface angle (°)
6	$\delta$	Wave angle (°)
7	$p_2/p_1$	Pressure ratio
8	$\rho_2/\rho_1$	Density ratio
9	$T_2/T_1$	Temperature ratio
10	$p_{02}/p_{01}$	Stagnation pressure ratio

**3.11.2 arsolmw - Oblique shock relations given  $M_1$  and  $\delta$** 

```

SUBROUTINE AR11AA(G,M,D,RESULT,IERR)
  DOUBLE PRECISION G, M, D, RESULT(10)
  INTEGER IERR

```

Compute the oblique shock relations given a mach number  $M$  and the wave angle  $\delta$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M_1 \geq 1$ .
d	in	Wave angle $0 < \delta < 90$ .
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_1$  out of range.
- 3 Given  $\delta$  out of range.

**3.11.3 arsolpw - Oblique shock relations given  $p_2/p_1$  and  $\delta$** 

```

SUBROUTINE AR11AB(G,P,D,RESULT,IERR)
  DOUBLE PRECISION G, P, D, RESULT(10)
  INTEGER IERR

```

Compute the oblique shock relations given the pressure ratio  $p_2/p_1$  and the wave angle  $\delta$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $p_2/p_1 > -(\gamma - 1)/(\gamma + 1)$ .
d	in	Wave angle $0 < \delta < 90$ .
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $p_2/p_1$  out of range.
- 3 Given  $\delta$  out of range.

**3.11.4** `arsoldw` - Oblique shock relations given  $\rho_2/\rho_1$  and  $\delta$ 

```

SUBROUTINE AR11AC(G,DS,D,RESULT,IERR)
  DOUBLE PRECISION G, DS, D, RESULT(10)
  INTEGER IERR

```

Compute the oblique shock relations given the density ratio  $\rho_2/\rho_1$  and the wave angle  $\delta$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
<code>g</code>	in	Specific heat constant $\gamma$ .
<code>p</code>	in	Density ratio $0 < \rho_2/\rho_1 < (\gamma + 1)/(\gamma - 1)$ .
<code>d</code>	in	Wave angle $0 < \delta < 90$ .
<code>result</code>	out	Array with result properties as described in 9.
<code>ierr</code>	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $\rho_2/\rho_1$  out of range.
- 3 Given  $\delta$  out of range.

**3.11.5 arsoltw - Oblique shock relations given  $T_2/T_1$  and  $\delta$** 

```

SUBROUTINE AR11AD(G,A,D,RESULT,IERR)
  DOUBLE PRECISION G, A, D, RESULT(10)
  INTEGER IERR

```

Compute the oblique shock relations given the temperature ratio  $T_2/T_1$  and the wave angle  $\delta$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $T_2/T_1$ .
d	in	Wave angle $0 < \delta < 90$ .
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $T_2/T_1$  out of range.
- 3 Given  $\delta$  out of range.

**3.11.6** arsolp0w - Oblique shock relations given  $p_{02}/p_{01}$  and  $\delta$ 

```

SUBROUTINE AR11AE(G,PO,D,RESULT,IERR)
  DOUBLE PRECISION G, PO, D, RESULT(10)
  INTEGER IERR

```

Compute the oblique shock relations given the stagnation pressure  $p_{02}/p_{01}$  and the wave angle  $\delta$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p0	in	Stagnation pressure ratio $p_{02}/p_{01}$ .
d	in	Wave angle $0 < \delta < 90$ .
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $p_{02}/p_{01}$  out of range.
- 3 Given  $\delta$  out of range.
- 4 Iterative solver failed.

**3.11.7 arsolws - Oblique shock relations given  $\theta$  and  $\delta$** 

```

SUBROUTINE AR11AF(G,D,T,RESULT,IERR)
  DOUBLE PRECISION G, D, T, RESULT(10)
  INTEGER IERR

```

Compute the oblique shock relations given the deflection surface angle  $\theta$  and the wave angle  $\delta$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Deflection surface angle $0 < \theta < 90$ .
d	in	Wave angle $0 < \delta < 90$ .
result	out	Array with result properties as described in 9.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 3 Given  $\theta$  or  $\delta$  out of range.

**3.11.8 arsolms - Oblique shock relations given  $M_1$  and  $\theta$** 

```

SUBROUTINE AR11AG(G,M,T,STRONG,RESULT,IERR)
  DOUBLE PRECISION G, M, T, RESULT(10)
  LOGICAL STRONG
  INTEGER IERR

```

Compute the oblique shock relations given the mach number  $M_1$  and the deflection surface angle  $\theta$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $M_1 \geq 1$ .
t	in	Deflection surface angle $0 < \theta < 90$ .
result	out	Array with result properties as described in 9.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_1$  out of range.
- 3 Given  $\theta$  out of range.
- 4 Calculation failed.

## 3.12 Oblique Shock Limits

### 3.12.1 Introduction

This set of functions computes the angle limits where an oblique shock would become detached or where the downstream flow would become sonic.

The following properties are computed:

Table 10: Oblique limit properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number for which the limit applies.
2	$\delta_{\max}$	Maximum wave angle ( $^{\circ}$ ).
3	$\theta_{\max}$	Maximum deflection surface angle ( $^{\circ}$ ).

**3.12.2 arsolld - Compute maximum wave and deflection surface angle before shock detachment**

```

SUBROUTINE AR12AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(3)
  INTEGER IERR

```

Compute maximum wave and deflection surface angle before shock detachment given a mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M \geq 1$ .
result	out	Array with result properties as described in 10.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.12.3 arsol1s - Compute maximum wave and deflection surface angle that wil result in sonic downstream flow**

```

SUBROUTINE AR12AB(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(3)
  INTEGER IERR

```

Compute maximum wave and deflection surface angle that wil result in sonic downstream flow given a mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M \geq 1$ .
result	out	Array with result properties as described in 10.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

### 3.13 Prandtl-Meyer function

#### 3.13.1 Introduction

This function group contains a forward and inverse Prandtl-Meyer function, these two functions are separated from the expansion fan and normal shock function groups for convenience. The properties computed are as follows:

Table 11: Prandtl-Meyer properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number.
2	$v(M)$	Prandtl-Meyer function (°).
3	$\theta$	Mach angle (°).

**3.13.2 arspmm - Prandtl-Meyer properties given  $M$** 

```

SUBROUTINE AR13AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(3)
  INTEGER IERR

```

Compute the Prandtl-Meyer properties given a mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M \geq 1$ .
result	out	Array with result properties as described in 11.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.13.3 arspmv - Prandtl-Meyer properties given  $v(M)$** 

```

SUBROUTINE AR13AB(G,N,RESULT,IERR)
  DOUBLE PRECISION G, N, RESULT(3)
  INTEGER IERR

```

Compute the Prandtl-Meyer properties from the Prandtl-Meyer angle  $v(M)$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
n	in	Prandtl-Meyer angle $v(M) \leq 90 \left( \sqrt{\frac{\gamma+1}{\gamma-1}} - 1 \right)$ .
result	out	Array with result properties as described in 11.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 3 Given  $v(M)$  out of range.
- 4 Iterative solver failed.

**3.13.4 arspmt - Prandtl-Meyer properties given  $\theta$** 

```

SUBROUTINE AR13AC(G,T,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(3)
  INTEGER IERR

```

Compute the Prandtl-Meyer properties given a mach angle  $\theta$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Mach angle $0 \leq \theta \leq 90$ .
result	out	Array with result properties as described in 11.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $\theta$  out of range.

**3.13.5 arspmfm - Prandtl-Meyer angle from  $M$** 

DOUBLE PRECISION FUNCTION AR13AD(G,M)  
DOUBLE PRECISION G, M

Computes the Prandtl-Meyer angle  $v(M)$  from the given mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M \geq 1$ .

**Return value**

This function returns the Prandtl-Meyer angle  $v(M)$  for the given mach number  $M$  or NAN (Not-a-Number) if an error has occurred).

**3.13.6 arspmfv - Mach number from  $v(M)$** 

DOUBLE PRECISION FUNCTION AR13AE(G, V)  
 DOUBLE PRECISION G, V

Computes the mach number  $M$  given the Prandtl-Meyer angle  $v(M)$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
n	in	Prandtl-Meyer angle $v(M) \leq 90 \left( \sqrt{\frac{\gamma+1}{\gamma-1}} - 1 \right)$ .

**Return value**

This function returns the mach number  $M$  for the given mach Prandtl-Meyer angle  $v(M)$  or NAN (Not-a-Number) if an error has occurred).

### 3.14 Expansion Fan (Rarefaction Wave)

#### 3.14.1 Introduction

This class computes the thermodynamic properties of compressible gas flow over a wedge for a calorically perfect gas, as described by [naca1135]. It computes the following properties given the specific heat ratio  $\gamma$  and any of the up- or downstream mach number plus any of the other properties. After calling any of the evaluation functions the following properties will be available, where the subscript 1,2 refers to upstream and downstream, respectively;

The following properties are computed:

Table 12: Expansion fan properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M_1$	Upstream mach number.
2	$M_2$	Downstream mach number.
3	$p_2/p_1$	Pressure ratio.
4	$\rho_2/\rho_1$	Density ratio.
5	$T_2/T_1$	Temperature ratio.

**3.14.2 arsefm - Expansion fan properties given  $M_1$  and  $M_2$** 

```

SUBROUTINE AR14AA(G,M1,M2,RESULT,IERR)
  DOUBLE PRECISION G, M1, M2, RESULT(5)
  INTEGER IERR

```

Compute the expansion fan properties given  $M_1$  and  $M_2$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m1	in	Upstream mach number $M_1 \geq 1$ .
m2	in	Downstream mach number $M_2 > 0$ .
result	out	Array with result properties as described in 12.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_1$  or  $M_2$  out of range.

**3.14.3 arsefp - Expansion fan properties given  $p_2/p_1$  and either  $M_1$  or  $M_2$** 

```

SUBROUTINE AR14AB(G,P,M,IS_M2,RESULT,IERR)
  DOUBLE PRECISION G, P, M, RESULT(5)
  LOGICAL IS_M2
  INTEGER IERR

```

Compute the expansion fan properties given  $p_2/p_1$  and either  $M_1$  or  $M_2$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $p_2/p_1$ .
m	in	Either $M_1 \geq 1$ or $M_2 > 0$ depending on whether is_m2 is false or true, respectively.
is_m2	in	Whether the given m refers to $M_1$ or $M_2$ .
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_1$  or  $M_2$  out of range.
- 3 Given pressure ratio  $p_2/p_1$  out of range.

**3.14.4 arsefd - Expansion fan properties given  $\rho_2/\rho_1$  and either  $M_1$  or  $M_2$** 

```

SUBROUTINE AR14AC(G,D,M,IS_M2,RESULT,IERR)
  DOUBLE PRECISION G, D, M, RESULT(5)
  LOGICAL IS_M2
  INTEGER IERR

```

Compute the expansion fan properties given  $\rho_2/\rho_1$  and either  $M_1$  or  $M_2$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $\rho_2/\rho_1$ .
m	in	Either $M_1 \geq 1$ or $M_2 > 0$ depending on whether is_m2 is false or true, respectively.
is_m2	in	Whether the given m refers to $M_1$ or $M_2$ .
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_1$  or  $M_2$  out of range.
- 3 Given pressure ratio  $\rho_2/\rho_1$  out of range.

**3.14.5 arseft - Expansion fan properties given  $T_2/T_1$  and either  $M_1$  or  $M_2$** 

```

SUBROUTINE AR14AD(G,T,M,IS_M2,RESULT,IERR)
  DOUBLE PRECISION G, T, M, RESULT(5)
  LOGICAL IS_M2
  INTEGER IERR

```

Compute the expansion fan properties given  $T_2/T_1$  and either  $M_1$  or  $M_2$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $T_2/T_1$ .
m	in	Either $M_1 \geq 1$ or $M_2 > 0$ depending on whether is_m2 is false or true, respectively.
is_m2	in	Whether the given m refers to $M_1$ or $M_2$ .
result	out	Array with result properties as described in 12.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M_1$  or  $M_2$  out of range.
- 3 Given pressure ratio  $T_2/T_1$  out of range.

## 3.15 (Rayleigh-)Pitot Tube Relations

### 3.15.1 Introduction

Computes the mach number out of the corresponding pressure given or inverse. For the supersonic case it computes the Rayleigh-Pitot equation which takes the bow shock in front of the pitot tube into account.

The following properties are computed: For  $M < 1$  the Pitot pressure ratio  $p_0/p$  will be computed for  $M \geq 1$  the

Table 13: (Rayleigh-)Pitot properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number.
2	$p$	Pressure ratio, see below

Rayleigh-Pitot pressure ratio  $p_{02}/p_1$  will be computed.

**3.15.2 arsp<sub>tm</sub> - (Rayleigh-)Pitot relations given  $M$** 

```
DOUBLE PRECISION FUNCTION AR15AA(G,M,IERR)
  DOUBLE PRECISION G, M
  INTEGER IERR
```

Compute the Rayleigh-Pitot properties given a mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 13.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**Return Values**

The pressure ratio  $p_0/p$  or  $p_{02}/p_1$  or NAN on error.

**3.15.3 arsptp - (Rayleigh-)Pitot relations given  $p_0/p$  or  $p_{02}/p_1$** 

```
DOUBLE PRECISION FUNCTION AR15AB(G,P0,IS_SUB,IERR)
  DOUBLE PRECISION G, P0
  LOGICAL IS_SUB
  INTEGER IERR
```

Compute the Rayleigh-Pitot properties given a one of the pressure ratios  $p_0/p$  or  $p_{02}/p_1$ .

**Performance**

- Fixed if is\_sub is true.
- Iterative if is\_sub is false.

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p0	in	The pressure ratio $p_0/p \geq 1$ or $p_{02}/p_1 \geq ((1+\gamma)/2)^{\gamma/(\gamma-1)}$ depending upon is_sub.
is_sub	in	Whether p0 refers to a Pitot pressure fraction (true) or to a Rayleigh-Pitot pressure fraction (false).
result	out	Array with result properties as described in 13.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given pressure ratio out of range.
- 3 Iterative solver failed.

**Return Values**

The Mach number  $M$  or NAN on error.

## 3.16 Reflected Shock Waves

### 3.16.1 Introduction

This function group computes the mach number of a reflected shock wave as given in [JDAnderson1982].

The following properties are computed:

Table 14: Reflected shock wave properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number of incident shock wave
2	$M'$	Mach number of reflected shock wave

**3.16.2 arsrms - Reflected shock wave mach number given  $M$** 

```
DOUBLE PRECISION FUNCTION AR16AA(G,MS,IERR)
  DOUBLE PRECISION G, MS
  INTEGER IERR
```

Computes the reflected shock wave mach number given  $M'$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
ms	in	Incident mach number $M \geq 1$ .
result	out	Array with result properties as described in 14.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**Return values**

The reflected shock wave mach number  $M'$  or NAN on error.

**3.16.3 arsrsmr - Incident shock wave mach number given  $M'$** 

```
DOUBLE PRECISION FUNCTION AR16AB(G,MR,IERR)
  DOUBLE PRECISION G, MR
  INTEGER IERR
```

Computes the incident shock wave mach number given  $M'$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Incident mach number $M' > 0$ .
result	out	Array with result properties as described in 14.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M'$  out of range.
- 3 Iterative solver failed.

**Return values**

The incident shock wave mach number  $M$  or NAN on error.

## 3.17 Quasi-2D Conical Flow

### 3.17.1 Introduction

This function group computes a solution to the *Taylor-Maccoll* equation for axis symmetric flow around a cone as for example described in [JDAnderson1982], that is:

$$\frac{\gamma-1}{2} \left[ 1 - V_r'^2 - \left( \frac{dV_r'}{d\theta} \right)^2 \right] \left[ 2V_r' + \frac{dV_r'}{d\theta} \cot\theta + \frac{d^2V_r'}{d\theta^2} \right] - \frac{V_r'}{d\theta} \left[ V_r' \frac{dV_r'}{d\theta} + \frac{dV_r'}{d\theta} \frac{d^2V_r'}{d\theta^2} \right] = 0$$

The solution to the above can be found given any combination of: the deflection surface angle  $\theta$  of the cone, an approximated wave angle  $\delta$  (i.e. using oblique shock relations) and the upstream mach number  $M$ . The solution is computed numerically using a Runge-Kutta method of the 4th order.

The following properties are computed:

Table 15: Conic shock properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$\theta$	Shock angle (°)
3	$\sigma$	Cone angle (°)

**3.17.2 arscmw - Conical flow given  $M$  and  $\delta$** 

```

SUBROUTINE AR17AA(G,M,W,RESULT,IERR)
  DOUBLE PRECISION G, M, W, RESULT(3)
  INTEGER IERR

```

Solve the conical flow given a mach number  $M$  and wave angle  $\delta$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M \geq 1$ .
w	in	Wave angle $0 < \delta < 90$ .
result	out	Array with result properties as described in 15.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.
- 3 Given  $\delta$  out of range.
- 4 Iterative solver failed.

**3.17.3 arscoms - Conical flow given  $M$  and  $\theta$** 

```

SUBROUTINE AR17AB(G,M,S,RESULT,IERR)
  DOUBLE PRECISION G, M, S, RESULT(3)
  INTEGER IERR

```

Solve the conical flow given a mach number  $M$  and deflection surface angle  $\theta$ .

**Performance**

Iterative

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M \geq 1$ .
s	in	Deflection surface angle $0 < \theta < 90$ .
result	out	Array with result properties as described in 15.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.
- 3 Given  $\theta$  out of range.
- 4 Iterative solver failed.

### 3.18 Moving Normal Shock Waves

Moving normal shock waves refer to normal shock waves in linear motion axis symmetric to the flow direction. Two sets of functions are available, one computes the thermodynamic properties of moving normal shock waves as described and the other set computes the mechanical/dynamic properties of such shock waves. These are separated as the functions computing the mechanical properties will require additional arguments in comparison to the thermodynamic property functions.

### 3.19 Moving Normal Shock Waves (Thermodynamic Properties)

#### 3.19.1 Introduction

This function group computes the thermodynamic properties of a moving normal shock wave.

The following properties are computed:

Table 16: Moving normal shock wave thermodynamic properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$p_2/p_1$	Pressure ratio
3	$\rho_2/\rho_1$	Density ratio
4	$T_2/T_1$	Temperature ratio

**3.19.2 arsmnsm - Moving shock relations given  $M$** 

```

SUBROUTINE AR18AA(G,M,RESULT,IERR)
  DOUBLE PRECISION G, M, RESULT(4)
  INTEGER IERR

```

Compute the moving normal shock wave relations given the mach number  $M$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $M > 0$ .
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.19.3 arsmnsp - Moving shock relations given  $p_2/p_1$** 

```
SUBROUTINE AR18AB(G,P,RESULT,IERR)
  DOUBLE PRECISION G, P, RESULT(4)
  INTEGER IERR
```

Compute the moving normal shock wave relations given the pressure ratio  $p_2/p_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
p	in	Pressure ratio $p_2/p_1 > (1 - \gamma)/(\gamma + 1)$ .
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $p_2/p_1$  out of range.

**3.19.4 arsmnsd - Moving shock relations given  $\rho_2/\rho_1$** 

```
SUBROUTINE AR18AC(G,P,RESULT,IERR)
  DOUBLE PRECISION G, D, RESULT(4)
  INTEGER IERR
```

Compute the moving normal shock wave relations given the density ratio  $\rho_2/\rho_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
d	in	Density ratio $\rho_2/\rho_1 > -(\gamma^2 - 1)/(\gamma^2 + 1)$ .
result	out	Array with result properties as described in 16.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $\rho_2/\rho_1$  out of range.

**3.19.5 arsmnst - Moving shock relations given  $T_2/T_1$** 

```

SUBROUTINE AR18AD(G,T,RESULT,IERR)
  DOUBLE PRECISION G, T, RESULT(4)
  INTEGER IERR

```

Compute the moving normal shock wave relations given the temperature ratio  $T_2/T_1$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
t	in	Temperature ratio $T_2/T_1 > (\gamma^2 + 1)/(\gamma + 1)^2$ .
result	out	Array with result properties as described in 16.
ierr	out	( <i>optional</i> ) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Computed  $M$  out of range.
- 3 Given  $T_2/T_1$  out of range.

## 3.20 Moving Normal Shock Waves (Dynamic Properties)

### 3.20.1 Introduction

This function group computes the mechanic/dynamic properties of a moving normal shock wave. These not only require the specific heat constant  $\gamma$  but also the speed of sound in the latter medium  $a_0$ .

The following properties are computed:

Table 17: Moving normal shock waves dynamic properties

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$p_2/p_1$	Pressure ratio
2	$V$	Velocity
3	$U_P$	Max-motion velocity, downstream

**3.20.2 arsmnvp - Dynamic moving shock relations given  $p_2/p_1$** 

```

SUBROUTINE AR19AA(G,A0,P,RESULT,IERR)
  DOUBLE PRECISION G, A0, P, RESULT(3)
  INTEGER IERR

```

Compute the dynamic moving normal shock wave relations given the the pressure ratio  $p_2/p_1$  and the speed of sound  $a_0$  of the medium.

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
a0	in	Speed of sound in the medium $a_0 > 0$ .
p	in	Pressure ratio $p_2/p_1 > (\gamma - 1)/(\gamma + 1)$ .
result	out	Array with result properties as described in 17.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $a_0$  out of range.
- 3 Given  $p_2/p_1$  out of range.

**3.20.3 arsmnvw - Dynamic moving shock relations given  $V$** 

```

SUBROUTINE AR19AB(G,A0,W,RESULT,IERR)
  DOUBLE PRECISION G, A0, W, RESULT(3)
  INTEGER IERR

```

Compute the dynamic moving normal shock wave relations given the the velocity  $V$  and the speed of sound  $a_0$  of the medium.

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
a0	in	Speed of sound in the medium $a_0 > 0$ .
w	in	Velocity $V > 0$ .
result	out	Array with result properties as described in 17.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $a_0$  out of range.
- 3 Computed  $p_2/p_1$  out of range.
- 4 Given  $V$  out of range.

**3.20.4 arsmnvup - Dynamic moving shock relations given  $U_p$** 

```

SUBROUTINE AR19AC(G,AO,UP,RESULT,IERR)
  DOUBLE PRECISION G, AO, UP, RESULT(3)
  INTEGER IERR

```

Compute the dynamic moving normal shock wave relations given the mass-motion velocity  $U_p$  and the speed of sound  $a_0$  of the medium.

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
a0	in	Speed of sound in the medium $a_0 > 0$ .
up	in	Maxx-motion velocity $U_p > -(2\sqrt{2}a_0\sqrt{\gamma(\gamma^2 + 2\gamma - 1)})/(\gamma + 1)$ .
result	out	Array with result properties as described in 17.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $a_0$  out of range.
- 3 Computed  $p_2/p_1$  out of range.
- 4 Given  $U_p$  out of range.

### 3.21 Karman-Tsien Pressure Correction Coefficient

#### 3.21.1 Introduction

The *Karman-Tsien* pressure correlation coefficient is defined as:

$$C_p = \frac{C_{p0}}{\sqrt{1-M^2} + \frac{1}{2} \left( \frac{M^2}{1+\sqrt{1-M^2}} \right) C_{p0}}$$

Where  $C_{p0}$  the incompressibility coefficient.

The following properties are computed:

Table 18: Karman-Tsien property table

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$C_p$	Pressure correction coefficient
3	$C_{p0}$	Incompressibility coefficient

**3.21.2 arckarcp - Karman-Tsien pressure correction given  $M$  and  $C_{p0}$** 

```

SUBROUTINE AR20AA(G,M,C,RESULT,IERR)
  DOUBLE PRECISION G, M, C, RESULT(3)
  INTEGER IERR

```

Compute the Karman-Tsien pressure correction coefficient relations given the mach number  $M$  and the the incompressibility coefficient  $C_{p0}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $0 < M < 0.8$ .
cin	in	Incompressibility coefficient $C_{p0}$ .
result	out	Array with result properties as described in 18.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.21.3 arckarci - Karman-Tsien pressure correction given  $M$  and  $C_p$** 

```

SUBROUTINE AR2OAB(G,M,CP,RESULT,IERR)
  DOUBLE PRECISION G, M, CP, RESULT(3)
  INTEGER IERR

```

Compute the Karman-Tsien pressure correction coefficient relations given the mach number  $M$  and the the Karman-Tsien pressure correction coefficient  $C_p$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $0 < M < 0.8$ .
cp	in	Pressure correction coefficient $C_p$ .
result	out	Array with result properties as described in 18.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

## 3.22 Laitone Pressure Correction Coefficient

### 3.22.1 Introduction

The *Laitone* pressure correlation coefficient is defined as:

$$C_p = \frac{C_{p0}}{\sqrt{1 - M^2} + \left( M^2 \frac{1 + (\gamma - 1)/2 \times M^2}{2\sqrt{1 - M^2}} \right) C_{p0}}$$

Where  $C_{p0}$  the incompressibility coefficient.

The following properties are computed:

Table 19: Laitone property table

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$C_p$	Pressure correction coefficient
3	$C_{p0}$	Incompressibility coefficient

**3.22.2 arclai cp - Laitone pressure correction given  $M$  and  $C_{p0}$** 

```

SUBROUTINE AR21AA(G,M,C,RESULT,IERR)
  DOUBLE PRECISION G, M, C, RESULT(3)
  INTEGER IERR

```

Compute the Laitone pressure correction coefficient relations given the mach number  $M$  and the the incompressibility coefficient  $C_{p0}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $0 < M < 0.8$ .
cin	in	Incompressibility coefficient $C_{p0}$ .
result	out	Array with result properties as described in 19.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.22.3 arclaiici - Laitone pressure correction given  $M$  and  $C_p$** 

```

SUBROUTINE AR21AB(G,M,CP,RESULT,IERR)
  DOUBLE PRECISION G, M, CP, RESULT(3)
  INTEGER IERR

```

Compute the Laitone pressure correction coefficient relations given the mach number  $M$  and the the Laitone pressure correction coefficient  $C_p$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $0 < M < 0.8$ .
cp	in	Pressure correction coefficient $C_p$ .
result	out	Array with result properties as described in 19.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

### 3.23 Prandtl-Glauert Pressure Correction Coefficient

#### 3.23.1 Introduction

The *Prandtl-Glauert* pressure correlation coefficient is defined as:

$$C_p = \frac{C_{p0}}{\sqrt{1-M^2}}$$

Where  $C_{p0}$  the incompressibility coefficient.

The following properties are computed:

Table 20: Prandtl-Glauert property table

<b>I</b>	<b>Property</b>	<b>Description</b>
1	$M$	Mach number
2	$C_p$	Pressure correction coefficient
3	$C_{p0}$	Incompressibility coefficient

**3.23.2 arcpglcp - Prandtl-Glauert pressure correction given  $M$  and  $C_{p0}$** 

```

SUBROUTINE AR22AA(G,M,C,RESULT,IERR)
  DOUBLE PRECISION G, M, C, RESULT(3)
  INTEGER IERR

```

Compute the Prandtl-Glauert pressure correction coefficient relations given the mach number  $M$  and the the incompressibility coefficient  $C_{p0}$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $0 < M < 0.8$ .
cin	in	Incompressibility coefficient $C_{p0}$ .
result	out	Array with result properties as described in 20.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.

**3.23.3 arcpglci - Prandtl-Glauert pressure correction given  $M$  and  $C_p$** 

```

SUBROUTINE AR22AB(G,M,CP,RESULT,IERR)
  DOUBLE PRECISION G, M, CP, RESULT(3)
  INTEGER IERR

```

Compute the Prandtl-Glauert pressure correction coefficient relations given the mach number  $M$  and the the Prandtl-Glauert pressure correction coefficient  $C_p$ .

**Performance**

Fixed

**Arguments**

Argument	Intent	Description
g	in	Specific heat constant $\gamma$ .
m	in	Mach number $0 < M < 0.8$ .
cp	in	Pressure correction coefficient $C_p$ .
result	out	Array with result properties as described in 20.
ierr	out	(optional) Return status code

**Status codes**

- 1 Specific heat ratio  $\gamma \leq 1$ .
- 2 Given  $M$  out of range.